

2. F is tangent to $\sigma(p)$ at ^{one} point, i.e., X_p consists of two pencils with focus p . In this case the locus of the lines in X_p will be two hyperplanes (Figure 9).

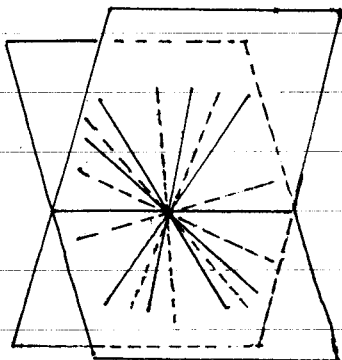


Figure 9

irrelevant here

Let l be the point s.t. $T_l(F) \supset \sigma(p)$.
 $F \cap \sigma(p) \subset F \cap T_l(F)$, which is a cone through l over a smooth quadric and) $F \cap \sigma(p)$ is a ^{non-smooth} quad-ratic curve in the α -plane $\sigma(p)$. \Rightarrow The only possibility of $F \cap \sigma(p)$ is the union of two lines.
 \Rightarrow Let $F \cap \sigma(p) = l_1 \cup l_2$. $\Rightarrow l_1$ & l_2 are pencils in \mathbb{P}^3 , and any line in $\tilde{\Phi}^{-1}(l_1)$ passes p since the line lies in $\sigma(p)$. $\Rightarrow \tilde{\Phi}^{-1}(l_1) = \sigma(p, h_1)$ and $\tilde{\Phi}^{-1}(l_2) = \sigma(p, h_2)$ for some α -planes h_1, h_2 .
 Here l_1 & l_2 are distinct since

F is tangent to $\sigma(p)$ at a point, and $F \cap \sigma(p)$ is not smooth at that point. \Rightarrow

3. F is tangent to $\sigma(p)$ along a line, i.e., X_p consists of one double line. In this case, the