

another pair  $P_k + P_e$ , so the points  $\mu_i, \mu_j$  are all distinct; these, then, are the 16 half-lattice points of  $A$ .

$$\begin{aligned} \textcircled{1} \quad h^0(P_i + P_j) &= \deg(P_i + P_j) - 2 (=g) + h^0(K - P_i - P_j) + 1 \\ &= 2 - 2 + h^0(K - P_i - P_j) + 1 \text{ by Riemann-Roch formula on } P_{245}. \end{aligned}$$

$$\textcircled{2} \quad K \neq P_i + P_j.$$

If not, consider the canonical mapping  $\iota_K$  defined

$$\text{by } \begin{array}{ccc} B & \longrightarrow & P' \\ \downarrow & & \downarrow \\ P & \longrightarrow & [W_1(P), W_2(P)] \end{array}, \quad W_1, W_2 \in H^0(B, \Omega').$$

Assume that  $W_2 = 0$  on  $P_i, P_j$ .

$\Rightarrow$  By P217,  $\iota_K$  is 2-1 map and since  $P_i \neq P_j$ ,  $P_i$  &  $P_j$  can not branch points. By the observation on P961 back page of note, they are not Weierstrass points.  $\Rightarrow$  Contradiction.  $\Rightarrow K \neq P_i + P_j$ .

$\textcircled{3}$  Since  $K \neq P_i + P_j$ , by the result on P247,  $h^0(K - P_i - P_j) = 0 \Rightarrow h^0(P_i + P_j) = 1$ , i.e.,  $\exists$  a unique section  $\sigma_\wedge$  of  $[P_i + P_j]$  s.t.  $(\sigma=0) = P_i + P_j$ .  
up to multiplication

$\Rightarrow$  If  $P_i + P_j \sim P_k + P_e$ , then  $[P_i + P_j] = [P_k + P_e]$ .

$\Rightarrow$  Since  $h^0(P_i + P_j) = h^0(P_k + P_e) = 1$ , and  $\exists \sigma_1, \sigma_2$  s.t.  $(\sigma_1=0) = P_i + P_j$ , and  $(\sigma_2=0) = P_k + P_e$ ,  $\sigma_1 = \alpha \sigma_2$ .

$\Rightarrow P_i + P_j = P_k + P_e$ .

$\Rightarrow$  The points  $\mu_{ij}$  are all distinct.