

$$\Rightarrow J_{f_t}(p) = e^{tA} \quad A = \begin{pmatrix} a_{11} & 0 & a_{21} & 0 \\ 0 & a_{11} & 0 & a_{21} \\ a_{12} & 0 & a_{22} & 0 \\ 0 & a_{12} & 0 & a_{22} \end{pmatrix}$$

\nearrow
real

$$\begin{aligned} \frac{\partial f}{\partial t} &= (a_{11}f_1 + a_{21}f_3) \frac{\partial}{\partial x_1} + (a_{11}f_2 + a_{21}f_4) \frac{\partial}{\partial y_1} \\ &\quad + (a_{12}f_1 + a_{22}f_3) \frac{\partial}{\partial x_2} + (a_{12}f_2 + a_{22}f_4) \frac{\partial}{\partial y_2} \\ &= a_{11}(f_1 + \sqrt{-1}f_2) \frac{\partial}{\partial z_1} + a_{21}(f_3 + \sqrt{-1}f_4) \frac{\partial}{\partial \bar{z}_1} \\ &\quad + a_{12}(f_1 + \sqrt{-1}f_2) \frac{\partial}{\partial z_2} + a_{22}(f_3 + \sqrt{-1}f_4) \frac{\partial}{\partial \bar{z}_2} \\ &= \frac{\partial}{\partial t} \begin{pmatrix} f_1 + \sqrt{-1}f_2 \\ f_3 + \sqrt{-1}f_4 \end{pmatrix} \\ \Rightarrow J_{f_t}(0) &= e^{t \begin{pmatrix} a_{11} & a_{21} \\ a_{12} & a_{22} \end{pmatrix}} \end{aligned} \quad + [\partial]$$

Now for t small, f_t will have a fixed point exactly where v has a zero, and by the holomorphic Lefschetz fixed-point formula,

$$L(f_t, 0) = \sum_{v(p)=0} \frac{1}{\det(I - B_p)}.$$

See P426

Since f_t is homotopic to the identity, f_t^* is the ident-