

binning with Sard's theorem, we can find an arc $r(t)$ s.t. $r(t) \in B(0, \frac{\delta}{2})$ for $t \neq 0$, $0 < t \leq \epsilon$. More precisely, $f(K) \cap B(0, \frac{\delta}{2})$ is open and dense, moreover path-connected, since $f(K) \cap B(0, \frac{\delta}{2})$ is an algebraic variety by the proper mapping theorem (let C be a compact subset in $B(0, \frac{\delta}{2})$). $f^{-1}(C) \subset U$ and $f^{-1}(C) \subset V \subset \bar{V} \subset U \Rightarrow f^{-1}(C)$ compact $\Rightarrow f|_{f^{-1}(B(0, \frac{\delta}{2}))}$ is proper and $f(K) \cap B(0, \frac{\delta}{2})$ has codimension $_{\mathbb{R}} \leq 2$)

~~For any fixed point $z_0 \in f(K) \cap B(0, \frac{\delta}{2})$, we can draw a curve $r(t)$ s.t. $r(0) = z_0$, $r(1) = z_1$, $0 \leq t \leq 1$, $|z_1| < |z_0|$. If \exists no curve $r(t)$ s.t. $r(0) = z_0$, $r(1) = 0$, and $r(t) \in f(K) \cap B(0, \frac{\delta}{2})$ for $0 \leq t < 1$. $\Rightarrow \exists \eta > 0$, s.t. $B(0, \eta) \subset f(K)$, which is impossible. \Rightarrow We have an arc $r(t)$ s.t. $r(t) \in f(K) \cap B(0, \frac{\delta}{2})$, $0 < t < 1$, $r($~~

Since $f(K) \cap B(0, \frac{\delta}{2})$ is an algebraic variety, \exists an open set \mathcal{O} s.t. $\bigcap_j (g_j = 0) = \mathcal{O} \cap f(K) \cap B(0, \frac{\delta}{2})$
 $\Rightarrow \exists$ a lot of lines from the origin which lie in $f(K) \cap B(0, \frac{\delta}{2})$ except the origin. \Rightarrow

Now we use the existence of good perturbations and continuity method to prove the

Transformation Law. Suppose $f = (f_1, \dots, f_n)$ and $g = (g_1, \dots, g_n)$ give holomorphic maps $f, g: \bar{U} \rightarrow \mathbb{C}^n$ with $f^{-1}(0) = \{0\} = g^{-1}(0)$. Suppose moreover that

$$g_i(z) = \sum_j a_{ij}(z) f_j(z)$$