

$$- L_{q_0} \cdot E_D \Rightarrow L_{q_3} \cdot E_D - p = L_{q_1} \cdot E_D - p + L_{q_2} \cdot E_D - p$$

$$\Rightarrow D_{q_3} = D_{q_1} + D_{q_2}$$

$\Rightarrow \{D_q\}_{q \in C}$ is a linear system

By ① & ②, $\{D_q = L_q \cdot E_D - p\}$ is a linear system of degree 2.

By Riemann-Roch,

$$\begin{aligned} h^0(D_q) &= 2 - 2 + 1 + h^0(K_B - D_q) \\ &= 2, \text{ since } \deg(K_B - D_q) \neq 0, \text{ and } K_B = D_q. \end{aligned}$$

For, by Prop 1,

if $K_B \neq D_q$, then $h^0(D_q) = 1$, which is impossible since C is 1-dimensional, and $\dim\{D_q\} = 1$.

In other words, every D_q is linearly equivalent to K_B . \Rightarrow In the book, the authors put $K_B = D_0$.

\Rightarrow

Thus the divisor $D = H \cdot E_D$ on B is of the form

$$D = 2D_0 + p.$$

$$\begin{aligned} \text{If } H \cdot E_D &= L_{q_1} \cdot E_D + L_{q_2} \cdot E_D - p = D_0 + p + D_0 + p - p \\ &= 2D_0 + p. \end{aligned}$$

\Rightarrow

Conversely, suppose that D is of ^{the} form $2D_0 + p$ for some $p \in \bigwedge_{E_D \text{ (or } B)}$. Then the divisors