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Give  $A$  the discrete topology, for open  $U \subset X$ ,  
 let  $\mathcal{A}(U)$  the group of all continuous maps of  $U$  into  $A$ .  
 $\Rightarrow$  For every connected open  $U$ ,  $\mathcal{A}(U) \cong A$ . whence the  
 name. "constant sheaf."  $\mathcal{A}(U_1 \cup U_2) \cong A \times A$ . direct product

② On any  $C^\infty$ -manifold  $M$ , we define sheaves  $C^\infty, C^*, \mathcal{Q}^p, \mathbb{Z}^p, \mathbb{Z}, \mathbb{Q}, \mathbb{R}$  and  $\mathbb{C}$  by

$C^\infty(U) = C^\infty$ -functions on  $U$ .

$C^*(U) =$  multiplicative group of non-zero  $C^\infty$ -functions on  $U$ .

$\mathcal{Q}^p(U) = C^\infty$ - $p$ -forms on  $U$ .

$\mathbb{Z}^p(U) =$  closed  $C^\infty$   $p$ -forms on  $U$ .  $\rightarrow \exists$  open connected set  $s.t. \mathcal{A}(U) \cong \mathbb{Z}, \dots, \mathbb{Q}$ .

$\mathbb{Z}(U), \mathbb{Q}(U), \mathbb{R}(U), \mathbb{C}(U) =$  locally constant  $\mathbb{Z}, \mathbb{Q}, \mathbb{R}$  or  $\mathbb{C}$ -valued functions on  $U$ .

③  $M$  complex manifold  $V \subset M$  analytic subvariety of  $M$ .  
 $E \rightarrow M$ : holomorphic vector bundle,  
 we define the sheaves  $\mathcal{O}, \mathcal{O}^*, \Omega^p, \mathcal{Q}^{p,q}, \mathbb{Z}_\partial^{p,q}, f_v$ ,  
 $\mathcal{O}(E)$ , and  $\mathcal{Q}^{p,q}$  by

$\mathcal{O}(U) =$  holomorphic functions on  $U$

$\mathcal{O}^*(U) =$  multiplicative group of non-zero holomorphic functions on  $U$

$\Omega^p(U) =$  holomorphic  $p$ -forms on  $U$ .

$\mathcal{Q}^{p,q}(U) = C^\infty$  forms of type  $(p,q)$  on  $U$

$\mathbb{Z}_\partial^{p,q}(U) = \bar{\partial}$ -closed  $C^\infty$  forms of type  $(p,q)$  on  $U$

$f_v(U) =$  holomorphic functions on  $U$  vanishing on  $V \cap U$ .

$\mathcal{O}(E)(U) =$  holomorphic sections of  $E$  over  $U$

$\mathcal{Q}^{p,q}(E)(U) = C^\infty$   $E$ -valued  $(p,q)$  forms over  $U$ .