

We get $r = -\frac{b_1 + b_2 k'(x_0)}{a_1 + a_2 k'(x_0)}$

Both $a_1 + a_2 k'(x_0)$ & $b_1 + b_2 k'(x_0)$ can not be zero since A and B are linearly independent.

Here we assumed that the slope of L_0 is $k'(x_0)$.

Thus we can conclude that $\exists r$ s.t. $f(x, y) + r g(x, y) = 0$ has L_0 as tangent at (x_0, y_0) .

E is tangent to L_0 at some point of P and

E passes through P . $\Rightarrow \#(E \cdot L_0) \geq 5$

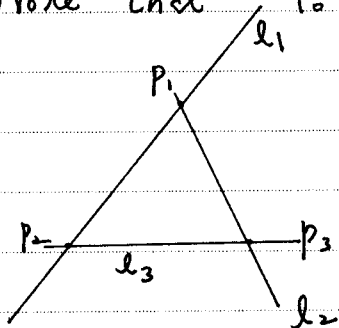
\Rightarrow Since $\deg E = 4$, by P64, $E \supset L_0$.

We may assume that $L_0 = (z_0 = 0)$.

\Rightarrow If f is a homogeneous polynomial representing E , then f is divisible by z_0 .

Let $f = z_0 g(z_0, z_1, z_2)$.

Note that $P_0 \cap P = \emptyset$.



Consider $l_1 \cap \{g=0\}$.

$\Rightarrow \#(l_1 \cdot \{g=0\}) \geq 4$.

\Rightarrow Since $\deg g = 3$, $\{g=0\} \supset l_1$.

$\Rightarrow g$ is divisible by g_1 , ^{homogeneous polynomial} representing l_1 .

\Rightarrow In the similar way,

we can conclude $g = g_1 g_2 g_3$,

where g_2 & g_3 are homogeneous polynomial representing l_2 and l_3 respectively.

$\Rightarrow f = z_0 g_1 g_2 g_3 \Rightarrow E = \Delta + L_0$.

$$\begin{array}{ccc} f_{P_0}(4) = f_P \otimes \mathcal{O}_P(4) & \xrightarrow{\otimes [-L_0] = [-H]} & f_{P_0}(3) = f_P \otimes \mathcal{O}_{P_0}(4-1) \\ \downarrow E & \longrightarrow & \downarrow E - L_0 = \Delta \end{array}$$