

The trivialization is what we want, i.e., $\varphi \Rightarrow$
 For $\alpha=1, \dots, n$, $e_{\lambda\alpha}(z)=1$, for

by \otimes map,

$$\varphi_{z+\lambda\alpha} \circ \varphi_z^{-1}(z, l) = (z, l).$$

\Rightarrow

Now suppose ω is any invariant integral form, positive of type $(1, 1)$. Choose a basis $\lambda_1, \dots, \lambda_{2n}$ for Λ over \mathbb{Z} such that in terms of dual coordinates x_1, \dots, x_{2n} on V

$$\omega = \sum_{\alpha=1}^n \delta_{\alpha} dx_{\alpha} \wedge dx_{\alpha+n}, \quad \delta_{\alpha} \in \mathbb{Z}.$$

Since ω is nondegenerate, $\delta_{\alpha} \neq 0$ for all α , and we can set

$$e_{\alpha} = \delta_{\alpha}^{-1} \lambda_{\alpha}, \quad \alpha=1, 2, \dots, n;$$

let z_1, \dots, z_n be linear coordinates on V dual to the basis e_1, \dots, e_n . Then as before we can write

$$(\lambda_1, \dots, \lambda_{2n}) = \begin{bmatrix} e_1 \\ \vdots \\ e_n \end{bmatrix} \Omega,$$

i.e.,

$$\begin{bmatrix} dz_1 \\ \vdots \\ dz_n \end{bmatrix} = {}^t \Omega (dx_1, \dots, dx_{2n})$$

with

$$\Omega = (\Delta_{\delta}, Z);$$