

Since $f(l_1, l_2) = f(l_2, l_1)$, f is two to one branched covering map.

Recall that ω_1 & ω_2 are Poincare duals of the pullbacks of the hyperplane class in \mathbb{P}^{2*} .

$$\begin{aligned}
 \deg W_1 &= \#(l \cap W_1) = \#(H \cap H \cap H \cap H \cap W_1) \text{ (since } H = \mathbb{P}^4 \text{ and } H \cap H \cap H \cap H = l) \\
 &= \#(H^4)_{W_1} = \int_{W_1} \tilde{H}^4 \text{ (} \tilde{H}^4 \text{ is the differential form corresponding to } H \text{)} \\
 &= \frac{1}{\deg f} \int_{\mathbb{P}^{2*} \times \mathbb{P}^{2*}} (f^* \tilde{H})^4 \\
 &= \frac{1}{\deg f} \int_{\mathbb{P}^{2*} \times \mathbb{P}^{2*}} (\tilde{\omega}_1 + \tilde{\omega}_2)^4 \text{ (} \tilde{\omega}_1, \tilde{\omega}_2 \text{ are the differential forms corresponding to } \omega_1, \omega_2 \text{ respectively)} \\
 &= \frac{1}{\deg f} \langle (\omega_1 + \omega_2)^4, [\mathbb{P}^{2*} \times \mathbb{P}^{2*}] \rangle \\
 &= \frac{1}{2} \langle 4\omega_1^2 \omega_2^2 + 2\omega_1^4 + 2\omega_2^4, [\mathbb{P}^{2*} \times \mathbb{P}^{2*}] \rangle \\
 &= \frac{1}{2} \cdot 6 = 3. \text{ where } [\mathbb{P}^{2*} \times \mathbb{P}^{2*}] \text{ is the fundamental class of } \mathbb{P}^{2*} \times \mathbb{P}^{2*}.
 \end{aligned}$$

□

Note that the subvariety $W_2 \subset W_1 \subset W$ is just the image under f of the diagonal $\Delta \cong \mathbb{P}^{2*}$ in $\mathbb{P}^{2*} \times \mathbb{P}^{2*}$, which is the branch locus of f .

Since a quadric of rank 1 is projectively isomor-