

\Rightarrow We proved the claim.

In general, since $\dim(\Lambda_0 \cap V_{b_i}) \leq \dim(\Lambda_0 \cap V_{b_j})$, if $i < j$, by doing the above process in turn, we get $\Lambda \in G(k, n)$ with $\dim(\Lambda \cap V_{b_i}) = i$ s.t. $\|\varphi(\Lambda) - \varphi(\Lambda_0)\| < \epsilon$.

In other words, do the process for the last $k \times (k + q_j - j)$ minor of Λ_0 in case j_1 is the largest number with $\dim(\Lambda_0 \cap V_{b_{j_1}}) > j_1$.

Next do the process for the second largest number with $\dim(\Lambda_0 \cap V_{b_{j_2}}) > j_2$.

For example, again $b_1 = 2$, $b_2 = 5$, $b_3 = 7$.
 $\Lambda_0 \in U_{11, 2, 4, 7}$.

$$\Lambda_0 = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 2 & 1 & 4 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\Rightarrow \dim(\Lambda_0 \cap V_{b_1}) = 2 \quad \dim(\Lambda_0 \cap V_{b_2}) = 3 \quad \dim(\Lambda_0 \cap V_{b_3}) = 3$$

First, the last 3×2 has rank 0. O.K.

Second, the last 3×4 has rank 0. \Rightarrow rank 1 = 3 - 2

Consider $\Lambda_1 = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 2 & 1 & 4 & \delta_1 & 0 & 0 & 0 \end{pmatrix}$

Third, the last 3×7 of Λ_1 has rank 1. \Rightarrow should be of rank 2 = 3 - 1.

Choose $\Lambda_2 = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & \delta_2 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 2 & 1 & 4 & \delta_1 & 0 & 0 & 0 \end{pmatrix} \Rightarrow \|\Lambda_2 - \Lambda_0\| < \epsilon.$