

$$\Gamma \quad \omega_{\bar{i}} = \frac{\omega_{\bar{i}}'}{\omega_0'} \quad \bar{i} \neq j$$

$$\begin{aligned} \frac{d\omega_{\bar{i}}}{\omega_{\bar{i}}} &= \frac{1}{\omega_{\bar{i}}} d\left(\frac{\omega_{\bar{i}}'}{\omega_0'}\right) = \frac{1}{\omega_{\bar{i}}} \frac{\omega_0' d\omega_{\bar{i}}' - \omega_{\bar{i}}' d\omega_0'}{\omega_0'^2} \\ &= \frac{1}{\omega_{\bar{i}}} \frac{1}{\omega_0'} d\omega_{\bar{i}}' - \frac{1}{\omega_{\bar{i}}} \frac{\omega_{\bar{i}}'}{\omega_0'^2} d\omega_0' \\ &= \frac{\omega_0'}{\omega_{\bar{i}}'} \frac{1}{\omega_0'} d\omega_{\bar{i}}' - \frac{\omega_0'}{\omega_{\bar{i}}'} \frac{\omega_{\bar{i}}'}{\omega_0'^2} d\omega_0' \\ &= \frac{d\omega_{\bar{i}}'}{\omega_{\bar{i}}'} - \frac{d\omega_0'}{\omega_0'} \end{aligned}$$

$$\bar{i} = j. \quad \omega_{\bar{j}} = \frac{1}{\omega_0'}$$

$$d\omega_{\bar{j}} = d\left(\frac{1}{\omega_0'}\right) = \frac{-d\omega_0'}{\omega_0'^2} = -d\omega_0' \cdot \frac{1}{\omega_0'^2}$$

$$\frac{d\omega_{\bar{j}}}{\omega_{\bar{j}}} = \omega_0' \frac{1}{\omega_0'^2} (-d\omega_0') = -\frac{d\omega_0'}{\omega_0'} \quad \sqcup$$

$$\begin{aligned} \Gamma \quad \omega &= \frac{d\omega_1}{\omega_1} \wedge \dots \wedge \frac{d\omega_n}{\omega_n} = \left(\frac{d\omega_1'}{\omega_1'} - \frac{d\omega_0'}{\omega_0'}\right) \wedge \left(\frac{d\omega_2'}{\omega_2'} - \frac{d\omega_0'}{\omega_0'}\right) \wedge \dots \wedge \left(\frac{d\omega_n'}{\omega_n'} - \frac{d\omega_0'}{\omega_0'}\right) \\ &\quad \dots \wedge \left(\frac{d\omega_n'}{\omega_n'} - \frac{d\omega_0'}{\omega_0'}\right) = \frac{d\omega_1'}{\omega_1'} \wedge \frac{d\omega_2'}{\omega_2'} \wedge \dots \wedge \left(-\frac{d\omega_0'}{\omega_0'}\right) \wedge \dots \wedge \left(\frac{d\omega_n'}{\omega_n'}\right) \\ &= (-1)^{\bar{j}} \left(\frac{d\omega_0'}{\omega_0'}\right) \wedge \left(\frac{d\omega_1'}{\omega_1'}\right) \wedge \dots \wedge \frac{d\omega_{\bar{j}}'}{\omega_{\bar{j}}'} \wedge \dots \wedge \left(\frac{d\omega_n'}{\omega_n'}\right). \quad \sqcup \end{aligned}$$

Thus we see that ω has likewise a single pole along the hyperplane ($z_0=0$), and consequently

$$K_{\mathbb{P}^n} = [(\omega)] = [-(n+1)H] \quad \text{every divisor of } \mathbb{P}^n \text{ is linearly equivalent to } H \subset \mathbb{P}^n.$$

$\Gamma \quad \omega$ is a globally defined meromorphic n -form on \mathbb{P}^n

with a single pole for each hyperplane ($z_{\bar{i}}=0$) for $\bar{i}=0, 1, \dots, n$.

$$\Rightarrow \omega \text{ is a meromorphic section of } K_{\mathbb{P}^n} \Rightarrow K_{\mathbb{P}^n} = [(\omega)] = [-(n+1)H].$$