

Γ $C_3 = \frac{5 \cdot 4 \cdot 6}{6} = 20$ choices of $\{L_i, L_j, L_k\}$
 Given a line X_p contained in such a hyperplane h
 as above, there are $X_{p_1}, X_{p_2}, X_{p_3}$ s.t.
 $h = \langle X_{p_1}, X_{p_2}, X_{p_3}, X_p \rangle \Rightarrow$ Choosing p_1, p_2, p_3 is
 choosing L_1, L_2, L_3 out of $\{L_i\}$. \square

Finally, since we have 16 points $p \in R$, 20 special
 tetrahedra containing each p as a vertex, and
 four vertices on each tetrahedron, we see that
 there are exactly 80 such hyperplane sections of
 Σ .

Γ For each p , \exists 20 hyperplanes.
 But, for example, p_1, p_2, p_3, p_4 produce $\langle X_{p_1}, X_{p_2}, X_{p_3}, X_{p_4} \rangle$
 four times. $\Rightarrow 16 \times 20 \div 4 = 80$ hyperplanes. \square

In sum, then,

The surface $\Sigma \subset \mathbb{P}^5$ contains 32 lines, forming
 two families of 16 disjoint lines, with each
 line meeting exactly six members of the opp-
 osite family. There are 80 hyperplanes in \mathbb{P}^5
 intersecting Σ in the sum of eight lines — four
 from each family — forming the configuration of
 Figure 19; and every line in Σ lies on 20