

\Rightarrow The volume form is given by $\alpha_1 \wedge \beta_1 \wedge \alpha_2 \wedge \beta_2 \dots$
 $\alpha_n \wedge \beta_n.$ □

□

φ (1,0) type.

$$\varphi = \alpha + i\beta$$

$$\begin{aligned} & (\alpha + i\beta) \left(\frac{\partial}{\partial x} - i \frac{\partial}{\partial y} \right) \\ &= \alpha \left(\frac{\partial}{\partial x} \right) + \beta \left(\frac{\partial}{\partial y} \right) + i \left(\beta \left(\frac{\partial}{\partial x} \right) - \alpha \left(\frac{\partial}{\partial y} \right) \right) = 0 \end{aligned}$$

$$\Rightarrow \alpha \left(\frac{\partial}{\partial x} \right) + \beta \left(\frac{\partial}{\partial y} \right) = 0$$

$$\beta \left(\frac{\partial}{\partial x} \right) - \alpha \left(\frac{\partial}{\partial y} \right) = 0$$

Suppose α & β are linearly dependent.

$$\alpha = a\beta. \quad a\beta \left(\frac{\partial}{\partial x} \right) + \beta \left(\frac{\partial}{\partial y} \right) = 0$$

$$\beta \left(\frac{\partial}{\partial x} \right) - a\beta \left(\frac{\partial}{\partial y} \right) = 0.$$

$$\Rightarrow a^2\beta \left(\frac{\partial}{\partial y} \right) + \beta \left(\frac{\partial}{\partial y} \right) = 0 \Rightarrow \beta \left(\frac{\partial}{\partial y} \right) = 0.$$

$$\Rightarrow \beta \left(\frac{\partial}{\partial x} \right) = 0 \Rightarrow \alpha = \beta = 0 \quad \text{Contradiction.}$$

$\Rightarrow \alpha$ & β are linearly independent. □