

Note, moreover, that if  $L$  is given by multipliers

$$e_{\lambda\alpha} \equiv 1, \quad e_{\lambda n+\alpha}(z) = e^{-2\pi i \bar{z}\alpha},$$

then  $\tau_\mu^* L$  can be given by multipliers

$$e'_{\lambda\alpha}(z) = e_{\lambda\alpha}(z+\mu) \equiv 1$$

$$\begin{aligned} e'_{\lambda n+\alpha}(z) &= e_{\lambda n+\alpha}(z+\mu) \\ &= e^{-2\pi i \bar{(z+\mu)}\alpha}, \end{aligned}$$

i.e.,  $e'_\lambda$  will differ from  $e_\lambda$  by multiplication by a constant  $e^{-2\pi i \bar{\mu}\alpha}$ .

¶ Note that, since  $\tau_\mu \circ \pi = \pi \circ \tau_\mu$ ,  $\tau_\mu^*(\pi^* L) = \pi^*(\tau_\mu^* L)$ . //

$$L = \frac{V \times \mathbb{C}}{(z, \zeta) \sim (z+\lambda, e_\lambda(z) \cdot \zeta)}.$$

$$\Rightarrow \tau_\mu^* L = \frac{V \times \mathbb{C}}{(z, \zeta) \sim (z+\lambda, e'_\lambda(z) \cdot \zeta)} \xrightarrow{\tau_\mu} \frac{V \times \mathbb{C}}{(z, \zeta) \sim (z+\lambda, e_\lambda(z) \cdot \zeta)}.$$

$$\Rightarrow \tau_\mu^*([z, \zeta]) = [z-\mu, \zeta] \quad \text{by definition of pull-back.}$$

$$\parallel \quad \quad \quad = [z-\mu+\lambda, e'_\lambda(z-\mu) \cdot \zeta]$$

$$\tau_\mu^*([z+\lambda, e_\lambda(z) \zeta]) = [z+\lambda-\mu, e_\lambda(z) \zeta]$$

$$\Rightarrow e'_\lambda(z-\mu) = e_\lambda(z) \Rightarrow e'_\lambda(z) = e_\lambda(z+\mu).$$

$$\text{Thus} \quad \begin{aligned} e'_{\lambda\alpha}(z) &= e_{\lambda\alpha}(z+\mu) = 1 \quad \text{for } \alpha = 1, \dots, n \\ e'_{\lambda n+\alpha}(z) &= e_{\lambda n+\alpha}(z+\mu) = e^{-2\pi i \bar{(z+\mu)}\alpha} \end{aligned}$$

⇒

Conversely, if  $L'$  is any line bundle with multipliers  $e'_{\lambda\alpha} \equiv 1$  and  $e'_{\lambda n+\alpha} \equiv c_\alpha \cdot e_{\lambda n+\alpha}$ ,  $c_\alpha \in \mathbb{C}^*$ , then setting