



$\Rightarrow F$  contains  $\sigma(p, h)$  since  $\deg F = 2$ .  $\Rightarrow X$  contains  $\sigma(p, h)$ .  $\Rightarrow$  Since  $X$  contains  $\sigma(p, h)$  for generic  $p \in C$ , and  $h$  is a plane,  $X$  contains  $\sigma(C, h)$ .  $\Rightarrow$  By the lemma on P762, it is impossible.  $\Rightarrow h \in R^*$ .

—

Finally, applying the same arguments to the dual Kummer surface  $S^* \subset \mathbb{P}^{3*}$ , we see that every point  $h^* \in R^*$  lies on six of the hyperplanes  $p^* \in R$ , or in other words every hyperplane  $h$  in  $\mathbb{P}^3$  corresponding to a point of  $R^*$  contains six of the points  $p_i$ : in sum, then, we have that:

Every hyperplane  $h \in R^*$  contains exactly six of the 16 double points of  $S$  and every double point of  $S$  lies on exactly six of the 16 hyperplanes  $h \in R^*$ .

□ In the argument above, we showed that each point  $p \in R$  lies on six hyperplanes which are elements