

Writing

$$\omega = \frac{\bar{c}}{2} (\varphi_1 \wedge \bar{\varphi}_1 + \varphi_2 \wedge \bar{\varphi}_2),$$

$$\zeta \wedge \omega = \frac{\bar{c}}{2} (\zeta_{11} + \zeta_{22}) \varphi_1 \wedge \bar{\varphi}_1 \wedge \varphi_2 \wedge \bar{\varphi}_2,$$

We see that ζ primitive implies $\zeta_{11} + \zeta_{22} = 0$.

⌈ Since " ζ primitive" means $\zeta \wedge \omega = 0$. ⌋

For the bilinear relation, $n=2$. $p+q = n-k = 2$

$$i^{p-q} (-1)^{(n-k)(n-k-1)/2} Q(\zeta, \bar{\zeta}) = -\bar{c}^0 Q(\zeta, \bar{\zeta}).$$

$$= -\int_M \zeta \wedge \bar{\zeta} = -\int_M (+ \zeta_{11} \bar{\zeta}_{22} \varphi_1 \wedge \bar{\varphi}_1 \wedge \bar{\varphi}_2 \wedge \varphi_2 + \zeta_{22} \bar{\zeta}_{11} \varphi_2 \wedge \bar{\varphi}_2 \wedge \bar{\varphi}_1 \wedge \varphi_1 + \bar{\zeta}_{21} \zeta_{12} \varphi_1 \wedge \bar{\varphi}_2 \wedge \varphi_2 \wedge \bar{\varphi}_1 + \bar{\zeta}_{12} \zeta_{21} \varphi_2 \wedge \bar{\varphi}_1 \wedge \varphi_1 \wedge \bar{\varphi}_2)$$

$$= -\int_M (-\zeta_{11} \bar{\zeta}_{22} - \zeta_{22} \bar{\zeta}_{11} + |\zeta_{12}|^2 + |\zeta_{21}|^2) \varphi_1 \wedge \bar{\varphi}_1 \wedge \varphi_2 \wedge \bar{\varphi}_2$$

$$= -\int_M (|\zeta_{11}|^2 + |\zeta_{22}|^2 + 2|\zeta_{12}|^2) \varphi_1 \wedge \bar{\varphi}_1 \wedge \varphi_2 \wedge \bar{\varphi}_2$$

$$= -\int_M (2|\zeta_{11}|^2 + 2|\zeta_{12}|^2) \left(\frac{2}{\bar{c}}\right)^2 \Phi$$

$$= + \frac{4}{1} \int_M 2(|\zeta_{11}|^2 + |\zeta_{12}|^2) \Phi > 0$$

$$\left(\begin{array}{l} \Phi = (-1) \left(\frac{\bar{c}}{2}\right)^2 \varphi_1 \wedge \varphi_2 \wedge \bar{\varphi}_1 \wedge \bar{\varphi}_2 = \left(\frac{\bar{c}}{2}\right)^2 \varphi_1 \wedge \bar{\varphi}_1 \wedge \varphi_2 \wedge \bar{\varphi}_2 \\ \text{See p. 10} \end{array} \right)$$