

Let $[f] \in \text{Ext}_0^1(M, N)$.

$$\begin{array}{ccc} E_1 & \xrightarrow{f} & N \\ \phi_1 \downarrow & \nearrow f' & \\ E_1' & & \end{array}$$

$$E_1/\partial E_2 \xrightarrow{\mu} N \oplus E_0$$

$$\downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow$$

$$E_1/\partial E_2 \xrightarrow{\psi} (f(e_1), \partial e_1)$$

$$\downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow$$

$$E_1'/\partial E_1' \xrightarrow{\psi} (f' \circ \phi_1(e_1), \partial \phi_1(e_1))$$

Thus define a map from $N \oplus E_0$ to $N \oplus E_0'$ by

$$n \oplus e_0 \mapsto n \oplus \phi_0(e_0).$$

\Rightarrow The diagram is commutative.

② independent of the choice of a representative in a class.

$$\text{Hom}(E_0, N) \xrightarrow{\delta} \text{Hom}(E_1, N) \xrightarrow{\delta} \text{Hom}(E_2, N)$$

\downarrow
 f, g

Suppose $\delta f = \delta g = 0$ and $f - g = \delta h$.