



By standard manifold theory, then X' is diffeomorphic to the product $I \times S_0$, and consequently S is diffeomorphic to S_0 : since X' is compact and the map $\gamma^{-1} \circ \pi$ is smooth, we can by a partition of unity lift the vector field $-\partial/\partial t$ on I to a vector field v on X' ; the flow $\varphi_t = \varphi_t(v)$ on X' will then map $\pi^{-1}(\gamma(t))$ diffeomorphically onto $\pi^{-1}(\gamma(0)) = S_0$.

By the arguments above, for each point $l \in X'$,
 \exists open set $U_l \ni l$ s.t. $U_l \cong \mathbb{C}^2 \times \mathbb{R}$.

$$(x, y, g(t, x, y), t) \leftrightarrow (x, y, t).$$

\Rightarrow Clearly we can lift the vector field $-\partial/\partial t$ on \mathbb{R} to $\mathbb{C}^2 \times \mathbb{R}$, and we get the lifted vector field on U_l ,

$$U_l \xrightarrow{\cong} \mathbb{C}^2 \times \mathbb{R} \quad T U_l \xrightarrow{\cong} T(\mathbb{C}^2 \times \mathbb{R})$$

$$\searrow \quad \swarrow \quad \Rightarrow \quad \searrow \quad \swarrow$$

$$\mathbb{R} \quad \quad \quad \mathbb{R}$$