

$$\text{I} \quad f^* \omega = f^* \left(\frac{g(\omega)}{h(\omega)} d\omega \right) = \frac{g(z^v)}{h(z^v)} dz^v = \frac{g(z^v)}{h(z^v)} v z^{v-1} dz$$

$$\Rightarrow \text{ord}_p(f^* \omega) = \# \text{ of multiplicities at } p \\ = (v-1) + v \cdot \text{ord}_{f(p)}(\omega)$$

$\text{ord}_{f(p)}(\omega) = \# \text{ of multiplicities at } f(p).$

See P130 for the definition of ord . We may take z as a local defining function for 0 (p in S) at 0 , & ω " " for 0 ($f(p)$ in S'). \square

This implies the equation of divisors on S

$$(f^* \omega) = f^*(\omega) + \sum_{p \in S} (v(p)-1) \cdot p$$

i.e., $K_S = f^* K_{S'} + B,$

$$\deg K_S = n \cdot \deg K_{S'} + \sum_{p \in S} (v(p)-1).$$

$$\text{II} \quad \text{ord}_p(f^* \omega) = v \cdot \text{ord}_{f(p)}(\omega) + (v-1).$$

Let $(\omega) = (\omega=0) = \sum a_i p_i'.$

\Rightarrow For each $p_i' \in S', \quad v(p) \cdot a_i = v(p) \cdot \text{ord}_{f(p)}(\omega)$
where $p \in f^{-1}(p_i').$

$$(f^* \omega) = \sum_{p \in S} \text{ord}_p(f^* \omega) \cdot p$$

$$= \sum_{p \in S} v(p) \cdot \text{ord}_{f(p)}(\omega) \cdot p + \sum_{p \in S} (v(p)-1) \cdot p$$

$$= \sum_{p \in S} (v(p)-1) \cdot p + \sum_{p \in S} v(p) \cdot \text{ord}_{f(p)}(\omega) \cdot p.$$