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We are going to compute a section of S^* over $G(2,4)$.

To do this, first we have to compute the transition functions for S.

$$\begin{array}{c} S \subset G(2,4) \times \mathbb{C}^4 \\ \downarrow \\ G(2,4). \end{array}$$

$U_{12}, U_{13}, U_{14}, U_{23}, U_{24}, U_{34}$

$$U_{12} \longrightarrow \mathbb{C}^{2(4-2)} = \mathbb{C}^4$$

$$\Lambda \longmapsto \begin{pmatrix} 1 & 0, & z_1, & z_2 \\ 0 & 1, & z_3, & z_4 \end{pmatrix} \longmapsto \begin{pmatrix} z_1, & z_2 \\ z_3, & z_4 \end{pmatrix}$$

$$U_{13} \longrightarrow \mathbb{C}^4$$

$$\Lambda \longmapsto \begin{pmatrix} 1, & w_1, & 0, & w_2 \\ 0, & w_3 & 1, & w_4 \end{pmatrix} \longmapsto \begin{pmatrix} w_1, & w_2 \\ w_3, & w_4 \end{pmatrix}$$

$$\mathbb{C}^4 \longleftarrow U_{12} \cap U_{13} \longrightarrow \mathbb{C}^4$$

$$\begin{pmatrix} 1, & w_1 & 0, & w_2 \\ 0, & w_3 & 1, & w_4 \end{pmatrix} \longleftarrow\!\shortmid \Lambda \longmapsto \begin{pmatrix} 1, & 0 & z_1, & z_2 \\ 0 & 1, & z_3, & z_4 \end{pmatrix}$$

$$\Rightarrow \begin{pmatrix} 1 & z_1 \\ 0 & z_3 \end{pmatrix}^{-1} \begin{pmatrix} 1, & 0, & z_1, & z_2 \\ 0, & 1, & z_3, & z_4 \end{pmatrix} = \begin{pmatrix} 1, & w_1, & 0, & w_2 \\ 0, & w_3, & 1 & w_4 \end{pmatrix}$$