

Proof. By the Riemann - Roch theorem

$$h^0(D) = \deg D - g + 1 + i(D) = 1,$$

so the only meromorphic functions with polar divisor  $D$  are the constants.