

\mathbb{R} T_E is a smoothing of T_E .

$$\Rightarrow T_E(\varphi) = \int_M T_E \wedge \varphi = \int_E \varphi$$

$$\Rightarrow T_E(T_E) = \int_E T_E = \int_M T_E \wedge T_E = E \cdot E \text{ by Poincaré duality P56 ~ P59.}$$

\Rightarrow If T_E is positive, then $\int_E T_E \geq 0$, but $E \cdot E = -1$.

\Rightarrow Contradiction. \sqcup

The intuitive reason for this is that T_E is a smooth form supported in ϵ -tubular neighborhood of E , and so T_E has to do with the shape of the normal bundle of E .

\mathbb{R} $T_E(\varphi) = 0$ if $\text{supp } \varphi \subset E^c$. $\text{supp } T_E \subset \epsilon$ -tubular nbd of E , roughly speaking. \sqcup

To say that T_E is positive would be something like saying that the normal bundle has positive curvature, which is not the case in this example.

$$\mathbb{R} \quad c_1(L) = \left[\frac{\sqrt{-1}}{2\pi} \Theta \right] \quad \text{by P141. compare with P148 } \sqcup$$

"Comment" $\begin{array}{ccc} L & \rightarrow & \text{line bundle.} \\ \downarrow & & \Rightarrow \\ M & \rightarrow & \text{curve} \end{array} \quad L = [D], \quad D \text{ is a divisor of } M.$

\Rightarrow By P141. Proposition 2, $c_1(L) = \eta_D \in H_{\text{DR}}^2(M)$.