

this end, for each p and q let

$$\{\psi_{p,q,\mu}\}$$

be a collection of $\bar{\partial}$ -closed (p,q) forms representing a basis for $H_{\bar{\partial}}^{p,q}(M)$, and let

$$\{\psi_{n-p,n-q,\mu}^*\}$$

be $\bar{\partial}$ -closed forms representing the dual basis for $H_{\bar{\partial}}^{n-p,n-q}(M)$ under the pairing

$$H_{\bar{\partial}}^{p,q}(M) \otimes H_{\bar{\partial}}^{n-p,n-q}(M) \longrightarrow \mathbb{C}$$

given by

$$\psi \otimes \varphi \longmapsto \int_M \psi \wedge \varphi. \quad \text{TF See p102 ~ p103 } \quad \sqcup$$

By the Künneth formula from Section 6 of Chapter 0 a basis for $H_{\bar{\partial}}^{n,n}(M \times M)$ is represented by the forms

$$\{\varphi_{p,q,\mu,\nu} = \pi_1^* \psi_{p,q,\mu} \wedge \pi_2^* \psi_{n-p,n-q,\nu}^*\},$$

and the dual basis for $H_{\bar{\partial}}^{n,n}(M \times M)$ is represented, as in the real case above, by

$$\{\varphi_{n-p,n-q,\mu,\nu}^* = \pi_1^* \psi_{n-p,n-q,\mu}^* \wedge \pi_2^* \psi_{p,q,\nu}\}.$$

TF See p103 ~ p105, & p419. \(\sqcup\)

The Dolbeault class η_{Δ} of the diagonal is

$$\eta_{\Delta} = \sum_{p,q,\mu} (-1)^{p+q} \varphi_{p,q,\mu,\mu}.$$

Now let $f: M \rightarrow M$ be a holomorphic map with isolated nondegenerate zeros; let $\Gamma_f = \{(p, f(p))\} \subset M \times M$ be its graph. If we compute the intersection number of Δ and