

hence that f and g are Weierstrass polynomials in z_n .

$$\mathbb{F} \{z' = 0\} = \{z_1 = \dots = z_{n-1} = 0\}.$$

Since $W \not\supset \{z' = 0\}$, at least one of f & g does not contain $\{z' = 0\}$, say f . Assume that $(g=0)$ contains $\{z' = 0\}$. Consider $af + g = g'$, $a \neq 0$.

$$\Rightarrow (g' = 0) \not\supset \{z' = 0\} \quad \text{And} \quad \{af + g = 0\} \cap \{g = 0\} \\ = \{f = 0\} \cap \{g = 0\} \Rightarrow \text{By P8, } f, g \text{ Weierstrass polys. } \quad \sqcup$$

Let $r = \alpha f + \beta g \neq 0 \in \mathcal{O}_{n-1}$ be the result of f and g .

$\mathbb{F} \quad f, g \in \mathcal{O}_{n-1}[Z_n]$. since f, g are Weierstrass polynomials. By the fact we did not prove (P9).

$$\exists \text{ relatively prime elements } \alpha, \beta \in \mathcal{O}_{n-1}[Z_n], r \in \mathcal{O}_{n-1}^{\times}, t \\ \alpha f + \beta g = r \in \mathcal{O}_{n-1}. \quad \sqcup$$

We claim that the image of W under the projection map $\pi: \mathbb{C}^n \rightarrow \mathbb{C}^{n-1}$ is just the locus of r . To see this, write

$$\alpha = hg + r$$

with the degree of r strictly less than the degree of g . Then $r = r f + (\beta + h f) g$.

Now, if, for some z in \mathbb{C}^{n-1} , r vanishes at z but f and g have no common zeros along the line $\pi^{-1}(z)$,