

coherent, for,

① $\text{Hom}(\mathcal{F}, \mathcal{O}^{(K)})$ is coherent,

$$\begin{aligned} & \mathcal{O}^{(r)} \rightarrow \mathcal{O}^{(K')} \rightarrow \mathcal{F} \rightarrow 0 \\ \Rightarrow & 0 \rightarrow \text{Hom}(\mathcal{F}, \mathcal{O}^{(K)}) \rightarrow \text{Hom}(\mathcal{O}^{(K')}, \mathcal{O}^{(K)}) \xrightarrow{\alpha} \text{Hom}(\mathcal{O}^{(r)}, \end{aligned}$$

$\mathcal{O}^{(K)})$. Once we prove $\text{Hom}(\mathcal{O}^{(K')}, \mathcal{O}^{(K)})$ is coherent, then since α is sheaf morphism, by the theorem 14 above, $\text{Hom}(\mathcal{F}, \mathcal{O}^{(K)}) = \ker \alpha$ is coherent.

$\text{Hom}(\mathcal{O}^{(K')}, \mathcal{O}^{(K)}) \cong \mathcal{O}^{(KK')}$ is coherent.

② $\text{Hom}(\mathcal{O}^{(K')}, \mathcal{G})$ is coherent, since $\text{Hom}(\mathcal{O}^{(K')}, \mathcal{G}) \cong \mathcal{G}^{(K')}$ by $\text{Hom}_R(R, M) \cong M$.

③ From $\mathcal{O}^{(p)} \rightarrow \mathcal{O}^{(q)} \rightarrow \mathcal{F} \rightarrow 0$, we get
 $0 \rightarrow \text{Hom}(\mathcal{F}, \mathcal{G}) \rightarrow \text{Hom}(\mathcal{O}^{(q)}, \mathcal{G}) \xrightarrow{\alpha} \text{Hom}(\mathcal{O}^{(p)}, \mathcal{G})$.

\Rightarrow Since $\text{Hom}(\mathcal{O}^{(q)}, \mathcal{G})$ and $\text{Hom}(\mathcal{O}^{(p)}, \mathcal{G})$ are coherent, and α is sheaf morphism, $\ker \alpha = \text{Hom}(\mathcal{F}, \mathcal{G})$ is coherent by 14 Theorem above again.