

where $l(v) = \langle v, \omega \rangle$ for all $v \in \mathbb{C}^n$.

Consider the following map which is isomorphic.

$$\begin{array}{ccc} S^* & \longrightarrow & Q \\ \downarrow & & \downarrow \\ G(n-k, n) & \longrightarrow & G(k, n) \\ \downarrow \Lambda^* & \longrightarrow & \downarrow \Lambda^\omega \end{array} \quad \omega \perp \Lambda$$

$$\begin{array}{ccc} (*\Lambda, \omega) & \longrightarrow & (\Lambda, \omega + \Lambda) \\ \uparrow \Lambda^* & & \uparrow \Lambda^\omega \end{array} \quad \begin{array}{c} S^* \\ Q \end{array} \quad ?$$

It remains to show that

$$Q = \bigcup_{\Lambda \in G(k, n)} \mathbb{C}^n / \Lambda, \text{ which was proved above}$$

" We want to express the dual bundle E^* of E in terms of transition functions of E . see p67

$$\varphi_\alpha: E|_{U_\alpha} \longrightarrow U_\alpha \times \mathbb{C}^n$$

$$\varphi_\alpha^*: E^*|_{U_\alpha} \longrightarrow U_\alpha \times \mathbb{C}^{n*} \text{ induced by } \varphi_\alpha \text{ naturally.}$$

$$\text{Let } g_{\alpha\beta} = \varphi_\alpha \circ \varphi_\beta^{-1}, \text{ and}$$

$$\psi_\alpha: E^*|_{U_\alpha} \longrightarrow U_\alpha \times \mathbb{C}^{n*} \xrightarrow{\cong} U_\alpha \times \mathbb{C}^n$$

defined by $f \cdot \varphi_\alpha^*$ $f \leftarrow$ defined naturally