

10.17.1992.

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Thus we have $2\bar{c} \langle [\Lambda, \Theta] \eta, \eta \rangle \geq 0$.

$$\Gamma \quad \bar{c} \langle \Lambda \Theta \eta, \eta \rangle \geq 0 \quad \bar{c} \langle \Theta \Lambda \eta, \eta \rangle \leq 0$$

$$\Rightarrow \bar{c} \langle [\Lambda, \Theta] \eta, \eta \rangle = \bar{c} \langle \Lambda \Theta \eta, \eta \rangle - \bar{c} \langle \Theta \Lambda \eta, \eta \rangle \geq 0 \quad \square$$

But now

$$\Theta = \Theta_{L^\mu \otimes E} = \Theta_E - \frac{2\pi}{\bar{c}} \mu \omega,$$

$$\text{and so } 2\bar{c} \langle [\Lambda, \Theta] \eta, \eta \rangle = 2\bar{c} \langle [\Lambda, \Theta_E] \eta, \eta \rangle - 4\pi\mu \langle [\Lambda, L] \eta, \eta \rangle \\ = 2\bar{c} \langle [\Lambda, \Theta_E] \eta, \eta \rangle - 4\pi\mu (n-p) \|\eta\|^2.$$

$$\Gamma \quad \Theta = \Theta_{L^\mu \otimes E} = \Theta_E - \frac{2\pi}{\bar{c}} \mu \omega \quad \text{from } \Theta_{L^\mu \otimes E} = \Theta_E + \frac{2\pi}{\bar{c}} \mu \omega$$

$$\bar{c} \langle [\Lambda, \Theta] \eta, \eta \rangle = \bar{c} \langle [\Lambda, 1 \otimes \Theta_E - \frac{2\pi}{\bar{c}} \mu \omega \otimes 1] \eta, \eta \rangle \\ = \bar{c} \langle [\Lambda, 1 \otimes \Theta_E] \eta, \eta \rangle - \bar{c} \langle [\Lambda, \frac{2\pi}{\bar{c}} \mu \omega \otimes 1] \eta, \eta \rangle$$

$$\text{But since } [\Lambda, \frac{2\pi}{\bar{c}} \mu \omega \otimes 1] \eta = \frac{2\pi\mu}{\bar{c}} [\Lambda, \omega \otimes 1] \eta \\ = \frac{2\pi\mu}{\bar{c}} [\Lambda, L] \eta = \frac{2\pi\mu}{\bar{c}} (n-p-\overset{0}{q}) \eta,$$

$$\bar{c} \langle [\Lambda, \frac{2\pi}{\bar{c}} \mu \omega \otimes 1] \eta, \eta \rangle \\ = 2\pi\mu (n-p) \langle \eta, \eta \rangle = 2\pi\mu (n-p) \|\eta\|^2.$$

$$\Rightarrow \bar{c} \langle [\Lambda, \Theta] \eta, \eta \rangle = \bar{c} \langle [\Lambda, 1 \otimes \Theta_E] \eta, \eta \rangle \\ - 2\pi\mu (n-p) \|\eta\|^2. \quad \square$$