

For the proof of ②, first of all,

Definition: If X is locally compact and μ is a Borel measure which is finite on all compact subsets of X , then μ is called a Radon measure. (See Donoghue. Distributions and Fourier Transforms. p24).

\Rightarrow By p42 ~ p51, \exists a ^{unique} Radon measure μ s.t

$$\Lambda(\varphi) = \int_G \varphi d\mu. \quad \varphi \in C_c^\circ(G). \quad \sqcup$$

Now let's go back to P17.

1c) At each point $x \in D$, let us write $V_m(x)$ for the infimum of those ξ for which the set $\{y; V(y) > \xi\}$ is of measure zero in a nbd of x . Then the condition to be fulfilled is:

$$V(x) = V_m(x) \quad \text{for each } x \in D.$$

$\overline{\text{IF}}$ Suppose $\xi > V_m(x)$. $\Rightarrow \{y; V(y) > \xi\}$ has measure zero in some nbd of x . \Rightarrow Almost all y satisfy $V(y) \leq \xi$, in the nbd of x . \sqcup

$V_m(x)$ is the limit of $\sup_u V(y)$ as we run through a sequence of nbds U having x as their only common point, the sup being taken in measure.

$\overline{\text{IF}}$