

$$\Rightarrow v = z \Rightarrow \sigma(z, l) = z$$

$$\Rightarrow \Omega_{[E]} = dd^c \log \frac{1}{\|z\|^2} = dd^c \log \frac{1}{\|z\|^2} = -dd^c \log \|z\|^2$$

By P24, if f is holomorphic, $\bar{\partial} \circ f^* = f^* \circ \bar{\partial}$ and, from the well-known fact $d \circ f^* = f^* \circ d$, $\partial \circ f^* = f^* \circ \partial$.

$$\begin{aligned} \pi': \tilde{U}_\epsilon - E &\longrightarrow \mathbb{P}^{n-1} \\ (z, l) &\longmapsto l. \end{aligned}$$

The Fubini-Study metric ω on \mathbb{P}^{n-1} is given by

$$\omega = \frac{i}{2\pi} \partial \bar{\partial} \log \|\tau\|^2, \quad \begin{array}{ccc} \tau: \mathbb{P}^{n-1} & \longrightarrow & \mathbb{C}^n \setminus \{0\} \\ l & \longmapsto & z \end{array}$$

$$\Rightarrow \pi'^* \omega = \frac{i}{2\pi} \pi'^* \partial \bar{\partial} \log \|\tau\|^2$$

$$= \frac{i}{2\pi} \partial \bar{\partial} \pi'^* \log \|\tau\|^2 = \frac{i}{2\pi} \partial \bar{\partial} \log \|\tau \circ \pi'\|^2$$

$$= \frac{i}{2\pi} \partial \bar{\partial} \log \|z\|^2 = dd^c \log \|z\|^2 = -\Omega_{[E]}$$

Note that ω is $(1,1)$ -form on \mathbb{P}^{n-1} , while $-\Omega_{[E]}$ is $(1,1)$ -form on $\tilde{U}_\epsilon - E$.

Since $\pi'^* \omega(v, \bar{v}) = \omega(\pi'_* v, \overline{\pi'_* v}) \geq 0$ (ω is positive definite), $-\Omega_{[E]} = \pi'^* \omega \geq 0$. \square

3. We have seen that $-\Omega_{[E]} = \pi'^* \omega$ on $\tilde{U}_\epsilon - E$; by continuity it follows that $-\Omega_{[E]} = \pi'^* \omega$ throughout \tilde{U}_ϵ , and in particular

$$-\Omega_{[E]}|_E = \omega > 0 \text{ on } E.$$