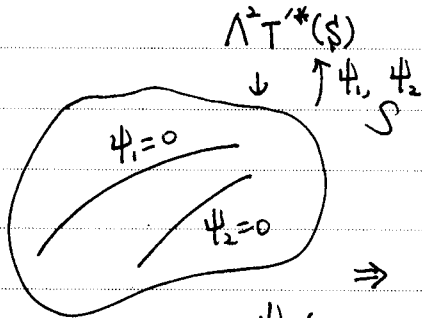


$\Rightarrow \Lambda^2 T^*(S)$ is not trivial, for, otherwise,

$\Lambda^2 T^*(S) \cong S \times \mathbb{C}, \Rightarrow H^0(S, \Omega^2) \cong H^0(S, \mathcal{O}) \cong \mathbb{C},$
which contradicts to $H^0(S, \Omega^2) = \langle \psi_1, \psi_2 \rangle.$

\Rightarrow



Choose p_1, p_2 & p_3 s.t

$p_2, p_3 \in (\psi_1 = 0),$ and $p_1 \notin (\psi_1 = 0).$

\Rightarrow Choose $\tau_i \in \Lambda^2 T^*(S).$

$\Rightarrow \psi_1(\tau_2) = \psi_1(\tau_3) = 0,$ and $\psi_1(\tau_1) \neq 0.$

\Rightarrow

$$\begin{pmatrix} \psi_1(\tau_1) & \psi_1(\tau_2) & \psi_1(\tau_3) \\ \psi_2(\tau_1) & \psi_2(\tau_2) & \psi_2(\tau_3) \end{pmatrix} \begin{pmatrix} a_1 \\ a_2 \\ a_3 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$

$\Rightarrow a_1 \psi_1(\tau_1) = 0 \Rightarrow a_1 = 0.$

\Rightarrow This implies that \exists no τ_p 's $\in \Lambda^2 T^*(S)$ s.t

$$\sum_{p \in Z} \langle \psi, \tau_p \rangle = 0 \quad \text{for all } \psi \in H^0(S, \Omega^2),$$

$Z = \{p_1, p_2, p_3\}.$

Thus the statement "if $\deg Z > P_g(S)$, then (E, S) always exists" is wrong, I think. \square

"We can prove the general result by following the same method above"

It remains to intrinsically interpret this relation, which we shall do in the next section.

Residues and Vector Bundles