

with distribution coefficients  $T_I$  defined by

$$T_I(\varphi) = \pm T(\varphi dx_I)$$

for  $\varphi \in C_c^\infty(\mathbb{R}^n)$ . Here  $I^\circ$  is the index set defined by  $*dx_I = \pm dx_{I^\circ}$ .

$$\Gamma \quad T \in \mathcal{D}'(\mathbb{R}^n) \Rightarrow T: A_c^{n-q}(\mathbb{R}^n) \longrightarrow \mathbb{C}.$$

$$T(dx_J) \in \mathbb{C} \text{ where } dx_J = dx_{j_1} \wedge \dots \wedge dx_{j_{n-q}}.$$

$$\text{If we let } T = \sum_{\#I=q} T_I dx_I,$$

$$T(\varphi dx_J) = \sum_{\#I=q} \pm T_I(\varphi) dx_I \wedge dx_J = \sum_{\#I=q} T_I(\varphi) dx.$$

$$\text{For example, } n=3, T = \begin{aligned} &T_{12} dx_1 \wedge dx_2 + T_{21} dx_2 \wedge dx_1 \\ &+ T_{23} dx_2 \wedge dx_3 + T_{32} dx_3 \wedge dx_2 \\ &+ T_{13} dx_1 \wedge dx_3 + T_{31} dx_3 \wedge dx_1 \end{aligned} \in A_c'(\mathbb{R}^3).$$

$$\begin{aligned} T(\varphi dx_1) &= T_{23}(\varphi) dx_2 \wedge dx_3 \wedge dx_1 + T_{32}(\varphi) dx_3 \wedge dx_2 \wedge dx_1 \\ &= (T_{23}(\varphi) - T_{32}(\varphi)) dx_1 \wedge dx_2 \wedge dx_3 \end{aligned}$$

$$\Rightarrow T(\varphi dx_1) = T_{23}(\varphi) - T_{32}(\varphi).$$

$\Rightarrow$  We assume that  $I = \{i_1, \dots, i_q\}$  with  $i_1 < i_2 < \dots < i_q$ .  $\square$

The smoothing

$$T_\epsilon = \sum_I (T_I)_\epsilon dx_I$$

satisfies

$$T_\epsilon(\varphi) \longrightarrow T(\varphi) \quad \text{as } \epsilon \rightarrow 0, \quad \varphi \in A_c^{n-q}(\mathbb{R}^n),$$

and

$$dT_\epsilon = d(T_\epsilon).$$

$$\Gamma \quad \text{Let } \varphi = \psi dx_1 \wedge \dots \wedge dx_{n-q}, \quad \psi \in C_c^\infty(\mathbb{R}^n). \Rightarrow T_\epsilon(\varphi) =$$