

The differentials d_1', d_2', \dots are induced from $U(V)$.
If we can show that $d_1' = d_2' = \dots = 0$, then

$$\begin{aligned} 'E_1^{p,q} &\cong 'E_2^{p,q} \cong \dots \cong 'E_\infty^{p,q} \\ &= 0, \text{ unless } p+q=n \end{aligned}$$

by the previous spectral sequence. This proves the theorem.

□ If we show that $d_1' = d_2' = \dots = d_r' = \dots = 0$, then
 $'E_1^{p,q} \cong \dots \cong 'E_\infty^{p,q} = H^{p,q}(M, \Omega^n) = H^q(M, \Omega^{n-p})$

By the previous spectral sequence

$$'E_2^{p,q} = 0 \text{ unless } p=0 \text{ and } q=n,$$

$$'E_2^{p+2,q+1} \rightarrow 'E_2^{p,q} \rightarrow 'E_2^{p+2,q-1} \Rightarrow \begin{aligned} 'E_3^{0,n} &= 'E_2^{0,n} \\ 'E_3^{p,q} &= 0 \text{ if } p \neq 0 \text{ or } q \neq n \end{aligned}$$

$$0 \rightarrow 'E_3^{0,n} \rightarrow 'E_3^{3,0} \Rightarrow 'E_3^{0,n} = 'E_4^{0,n} = \dots = 'E_\infty^{0,n} \text{ otherwise } 0.$$

$$\Rightarrow 'E_\infty^{p,q} = \begin{cases} H^p(M, \underline{\text{Ext}}_0^q(\mathcal{O}_Z, \Omega^n)) & \text{if } p=0 \text{ \& } q=n \\ 0 & \text{otherwise} \end{cases}$$

$$\Rightarrow H^0(M, \underline{\text{Ext}}_0^n(\mathcal{O}_Z, \Omega^n)) = 'E_\infty^{0,n} = H^n(M, \Omega^n) \text{ otherwise } 0 = H^q(M, \Omega^p)$$

$$\Rightarrow H^q(M, \Omega^p) = H^{p,q}(M) = 0 \text{ unless } p=q=n$$

$$\Rightarrow H^q(M, \Omega^p) = H^{p,q}(M) = 0 \text{ if } p \neq q. \quad \square$$

Step Two. Let $L \in H^{n-1}(M)$ be the cohomology class of a Kähler metric ω . The proof that $d_1' = d_2' = \dots = 0$ will use the hard Lefschetz theorem.