

We shall give the precise definitions and derive the finiteness theorem in a different way. Two effective divisors D_1, D_2 are algebraically equivalent in the strong sense, written

$$D_1 \equiv D_2,$$

if there is a connected parameter variety T with marked points $t_1, t_2 \in T$ and divisor D on $M \times T$ such that

$$D \cdot M \times \{t_i\} = D_i \quad (i=1, 2).$$

It is like a cobordism. \hookrightarrow

Intuitively, there is an algebraic family $D_t (t \in T)$ of divisors connecting D_1 and D_2 .

$$\hookrightarrow D \cdot M \times \{t\} = D_t. \quad \hookrightarrow$$

Two divisors D_1, D_2 are algebraically equivalent, written $D_1 \equiv D_2$, if there is a divisor D such that both of $D + D_i$ are effective and $D + D_1 = D + D_2$.

We will see in a minute that this is an equivalence relation compatible with the group structure on $\text{Div}(M)$.

$$\hookrightarrow D_1 \equiv D_2 \text{ \& \& } D_2 \equiv D_3 \stackrel{?}{\Rightarrow} D_1 \equiv D_3.$$

$$\Rightarrow D_1 + L = D_2 + L \text{ \& \& } D_2 + L' = D_3 + L'$$

$$\Rightarrow D_1 + L + L' = D_2 + L + L' = D_3 + L' + L \Rightarrow \text{By adding.}$$