

"A sheaf of \mathcal{O}_M -modules is a sheaf \mathcal{F} on M , s.t. for each open set $U \subseteq M$, the group $\mathcal{F}(U)$ is an $\mathcal{O}(U)$ -module, and for each inclusion of open sets $V \subseteq U$, the restriction homomorphism $\mathcal{F}(U) \rightarrow \mathcal{F}(V)$ is compatible with the module structures via the ring homomorphism $\mathcal{O}(U) \rightarrow \mathcal{O}(V)$.

A morphism $\mathcal{F} \rightarrow \mathcal{G}$ of sheaves of \mathcal{O} -modules is a morphism of sheaves, s.t. for each open set $U \subseteq M$, the map $\mathcal{F}(U) \rightarrow \mathcal{G}(U)$ is a homomorphism of $\mathcal{O}(U)$ -modules."

Given $\sigma \in H^0(M, \underline{\text{Ext}}^1_{\mathcal{O}}(\mathcal{G}, \mathcal{F}))$,
 $\sigma \in \underline{\text{Ext}}^1_{\mathcal{O}}(\mathcal{G}, \mathcal{F})(M)$.

For each U_α ,

$$\sigma|_{U_\alpha} \in \underline{\text{Ext}}^1_{\mathcal{O}}(\mathcal{G}(U), \mathcal{F}(U)).$$

\Rightarrow Since $\mathcal{G}(U)$ & $\mathcal{F}(U)$ are $\mathcal{O}(U)$ -modules,
 $\exists \mathcal{E}_\alpha$, $\mathcal{O}(U_\alpha)$ -module s.t

$$0 \rightarrow \mathcal{F}|_{U_\alpha} \rightarrow \mathcal{E}_\alpha \rightarrow \mathcal{G}|_{U_\alpha} \rightarrow 0$$

Since $\mathcal{O}(U_\alpha)$ is not equal to \mathcal{O} , we had better use a different trick.

For each point $x \in M$, $\sigma_x \in \underline{\text{Ext}}^1_{\mathcal{O}}(\mathcal{G}, \mathcal{F})_x$
 $= \underline{\text{Ext}}^1_{\mathcal{O}_x}(\mathcal{G}_x, \mathcal{F}_x)$

\Rightarrow Since \mathcal{G}_x & \mathcal{F}_x are \mathcal{O}_x -modules, $\exists \mathcal{E}_x$,
 \mathcal{O}_x -module s.t