

and the form

$$\Omega_{\pi^*L^k \otimes [-E]} = \Omega_{\pi^*L^k} + \Omega_{[-E]}$$

$$= k \Omega_{\pi^*L} + \Omega_{[-E]}$$

is positive everywhere in  $\tilde{U}_\epsilon$  and  $\tilde{M} - \tilde{U}_{2\epsilon}$ .

$$\mathbb{F} \quad \Omega_{\pi^*L^k \otimes [-E]} = \frac{i}{2\pi} \Theta_{\pi^*L^k \otimes [-E]} = -\frac{i}{2\pi} \partial \bar{\partial} \log \|s\|_{L^k}^2 + \frac{i}{2\pi} \partial \bar{\partial} \log \|\sigma\|_{[-E]}^2$$

$$= -\frac{i}{2\pi} \partial \bar{\partial} \log \|s\|_{L^k}^2 - \frac{i}{2\pi} \partial \bar{\partial} \log \|\sigma\|_{[-E]}^2$$

$$= \frac{i}{2\pi} \Theta_{\pi^*L^k} + \frac{i}{2\pi} \Theta_{[-E]} = \Omega_{\pi^*L^k} + \Omega_{[-E]}$$

where  $s: \tilde{M} \rightarrow \pi^*L^k$  a section which is nonzero.  
 $\sigma: \tilde{M} \rightarrow [-E]$

the metric on  $\pi^*L^k \otimes [-E]$  is induced as  
 $\langle \cdot, \cdot \rangle = \langle \cdot, \cdot \rangle_{\pi^*L^k} \cdot \langle \cdot, \cdot \rangle_{[-E]}$

In general,  $\Omega_{L_1 \otimes L_2} = \Omega_{L_1} + \Omega_{L_2}$  and

$$\Theta_{L_1 \otimes L_2} = \Theta_{L_1} + \Theta_{L_2}$$

$$\Rightarrow \Omega_{\pi^*L^k \otimes [-E]} = \Omega_{\pi^*L^k} + \Omega_{[-E]} = k \Omega_{\pi^*L} + \Omega_{[-E]}$$

Since  $\Omega_{\pi^*L}$  is positive in  $\tilde{M} - E$ , so  $\Omega_{\pi^*L}$  is positive in  $\tilde{M} - \tilde{U}_{2\epsilon}$ .  $\Omega_{[-E]}$  is positive on  $T'_x(E)$  and  $\Omega_{\pi^*L}$  is positive on  $T'_x(\tilde{M})/T'_x(E)$ .  $\Rightarrow$

- ①  $k \Omega_{\pi^*L} + \Omega_{[-E]}$  is positive on  $T'_x(\tilde{M})$  for all  $x \in E$ .
- ②  $k \Omega_{\pi^*L}$  is positive on  $\tilde{M} - \tilde{U}_{2\epsilon}$  and  $\Omega_{[-E]}$  is  $\geq 0$  on  $\tilde{M} - \tilde{U}_{2\epsilon}$ .

$\Rightarrow$  From ① & ②,  $\Omega_{\pi^*L^k \otimes [-E]}$  is positive everywhere in  $\tilde{U}_\epsilon$  and  $\tilde{M} - \tilde{U}_{2\epsilon}$ .