

from the complex manifold  $M$  to the algebraic variety  $N$  is given by a holomorphic map

$$f: M - V \longrightarrow N$$

defined on the complement of a subvariety  $V$  of codimension  $\geq 2$  or more in  $M$ .

Next, we would like to relate rational maps to  $\mathbb{P}^n$  to linear systems of divisors and sections of line bundles, as we have done with holomorphic maps. Let  $L \rightarrow M$  be a line bundle and  $\sigma_0, \dots, \sigma_n \in H^0(M, \mathcal{O}(L))$  a collection of linearly independent global holomorphic sections of  $L$ . Then the meromorphic functions

$$f_i = \frac{\sigma_i}{\sigma_0}$$

determines a rational map

$$f: M \longrightarrow \mathbb{P}^{n*}.$$

$$\begin{array}{ccccc} \Gamma & f: & M & \longrightarrow & \mathbb{P}^n & \longrightarrow & \mathbb{P}^{n*} \\ & & \downarrow \alpha & & & & \downarrow \\ & & x & \longmapsto & [1, f_1(x), \dots, f_n(x)] & \longmapsto & H \\ & & & & & & (a_0'' + a_1 f_1(x) + \dots + a_n f_n(x)) \\ & & & & & & \downarrow \\ & & & & & & 0 \end{array}$$

In terms of divisors, suppose  $|D_\lambda|_{\lambda \in \mathbb{P}^n}$  is a linear system on  $M$ . Let  $E$  be the fixed component of  $|D_\lambda|$  — that is, the largest effective divisor such that  $D_\lambda - E > 0$  for every  $\lambda$  — so that the divisors  $|D'_\lambda| = |D_\lambda - E|$  form a linear system with base locus of codimension at