

divisor $K' \in |K|$, $\phi^{-1}(K')$ has the finite cardinality, and
 $\dim \{D_1\} \times \{D_2\} = \dim |D_1| + \dim |D_2|$. Thus $\dim \{D_1 + D_2\}$
 $\geq \dim |D_1| + \dim |D_2| = h^0(D) - 1 + h^0(D') - 1 = h^0(D) + h^0(K-D) - 2$
 But $\dim \{K'\} = \dim |K| = h^0(K) - 1 \Rightarrow h^0(D) + h^0(K-D) - 2 <$
 $g-1 \Rightarrow h^0(D) + h^0(K-D) < g+1 \Rightarrow \text{Contradiction.}$

(\Leftarrow). From the argument above, it is clear. \Rightarrow

But by our lemma the points of a generic hyperplane section of $L_K(S)$ are in general position, and so $\geq h^0(D)$ can equal $d+2$ only if $D=0$, $D=K$, or L_K is not one to one.

Γ If $L_K: S \longrightarrow L_K(S) \subset \mathbb{P}^{g-1}$ is an embedding,

\Rightarrow Let $D' = L_K(D)$, $L_K(K) = K'$. \Rightarrow If $\geq h^0(D) = d+2$,
 $\geq h^0(D') = d+2 \Rightarrow \exists$ a generic hyperplane H in \mathbb{P}^{g-1}
 s.t. $H \cap \overset{\text{set of distinct points}}{L_K(S)} = K'$. \Rightarrow By the argument above,
 $\exists D_1, D_2$ s.t. $D_1 \in |D'|$ & $D_2 \in |K' - D'|$, $D_1 + D_2 = K'$.

\Rightarrow Since, p. 49, D_1 has the g points which must be linearly independent, which is not true, since D_1 lies in the hyperplane H .
 Thus the possibilities are ① L_K is not one to one (embedding) \uparrow
 to one, D is not special i.e.
 $h^0(K-D) = 0 \Rightarrow D = K$, for, if $K \neq D$.

\Rightarrow Since $\#(H \cap L_K(S)) = 2g-2$, if $D_1 \neq \emptyset \neq D_2$,
 then $\#D_1 \geq g-1$ or $\#D_2 \geq g-1$ ($\because \#D_1 + \#D_2 = 2g-2$).
 \Rightarrow By the lemma p. 49 $\dim \bar{D}_1 = g-1$ or.