

By multiplying $\underbrace{\psi \wedge \Omega^{n-p}}_{\text{by } (-1)^p}$, $\psi \wedge \Omega^{n-p} \geq 0$, since

$$T_\psi(\Omega^{n-p}) = T_\psi(\eta \wedge \bar{\eta}) \geq 0, \quad \Omega^{n-p} = \sum_i \eta_i \wedge \bar{\eta}_i, \text{ by}$$

$$\partial \bar{\partial} \log \|z\|^2 = \frac{\|dz\|^2}{\|z\|^2} = \frac{\sum dz_i \wedge d\bar{z}_i}{\|z\|^2} \quad \square$$

Definition. The Lelong number is

$$\Theta(T, p') = \frac{1}{\pi^{n-p}} \lim_{r \rightarrow 0} \Theta(T, p', r).$$

It is clear that $\Theta(T, p') \geq 0$ and is identically equal to zero in case T is a smooth current.

$$\square \quad \Theta(T, p', r) = \frac{1}{r^{2n-2p}} \int_{B[r]} \psi \wedge \omega^{n-p} \leq$$

$$\frac{1}{r^{2n-2p}} \int_{B[r]} M \, d\text{vol} = \frac{1}{r^{2n-2p}} M \times C_n r^{2n}$$

$$= M \times C_n r^{2p} \rightarrow 0 \quad \text{as } r \rightarrow 0. \quad \square$$

As indicated above

$$\Theta(T_Z, p') = \text{mult}_{p'}(Z)$$

for currents defined by analytic varieties.

Sketch of proof. By the proof of the previous lemma,