

moreover, since for any point $(q_1, \dots, q_n) \in \mathbb{C}^n$ sufficiently near $\pi_I(H_0)$, there is a hyperplane $H \in \mathcal{U}$ containing q_1, q_2, \dots, q_n , the image of \mathcal{U} under π_I contains an open set in \mathbb{C}^n .

"구성된 바귀것"

Remember that since H_0 meets with C in d distinct p_1, \dots, p_d , $\{p_1, \dots, p_d\}$ spans the hyperplane H_0 .

\Rightarrow For a point $(q_1, \dots, q_n) \in \mathbb{C}^n$ sufficiently near $\pi_I(H_0)$, consider the space spanned by q_1, \dots, q_n . If the space is not a hyperplane, by adding some p_i 's, we have a hyperplane containing q_1, \dots, q_n . Since the hyperplane H is very close to H_0 , $H \in \mathcal{U}$.

Here we used the fact that if p_1, \dots, p_e are linearly independent, then a set of points (q_1, \dots, q_e) which are very close to (p_1, \dots, p_e) is linearly independent. \square

Now let $D \subset \mathbb{C}^n$ be the locus of points (q_1, \dots, q_n) such that q_1, q_2, \dots, q_n are linearly dependent. Since C is nondegenerate, D is a proper analytic subvariety of \mathbb{C}^n , and so $\pi_I^{-1}(D)$ is likewise a proper subvariety of \mathcal{U} .

$$\begin{aligned} \Gamma \quad C \times C \times \dots \times C^n &\xrightarrow{\phi} \mathbb{C} \\ (q_1, q_2, \dots, q_n) &\longmapsto \det \begin{pmatrix} q_1 \\ \vdots \\ q_n \end{pmatrix} \end{aligned}$$

$\Rightarrow D = (\phi = 0)$ is a proper analytic subvariety since $\exists (q_1, \dots, q_n)$ which is linearly independent.

$\Rightarrow \pi_I^{-1}(D) = \mathcal{U} \cap (\phi \circ \pi_I = 0) \Rightarrow \pi_I^{-1}(D)$ is a subvar-