

is zero, too.  $\Rightarrow d_2 : H^p(B, R^{n-k}) \longrightarrow H^{p+2}(B, R^{n-k-1})$   
 $H^p(B, P^{n-k}) \oplus \dots \oplus H^p(B, L^q P^{n-k-2q}) \oplus \dots$   
 is zero.  $\sqcup$

"For the proof for  $d_3 = 0$ ."

As we saw above,  $d_2 = 0 \Rightarrow E_3^{p,q} = E_2^{p,q} = H^p(B, R^q)$ .  
 $\Rightarrow L^k : E_3^{p, n-k} = H^p(B, R^{n-k}) \longrightarrow H^p(B, R^{n+k}) = E_3^{p, n+k}$  is iso-  
 morphic.

$\dots n-k, \dots, n-1, \underset{\substack{| \\ \downarrow}}{n}, n+1, \dots, n+k \dots$

$\Rightarrow$  It will suffice to show that  $d_3 = 0$  on  $E_3^{p, n-k}$ .

$$H^p(B, R^{n-k}) = E_3^{p, n-k} = H^p(B, P^{n-k}) \oplus H^p(B, L P^{n-k-2}) \oplus \dots$$

$$\downarrow d_3$$

$$H^{p+3}(B, R^{n-k-2})$$

Again we have the following diagrams.

$$\begin{array}{ccc} H^p(B, P^{n-k}) & \xrightarrow{d_3} & H^{p+3}(B, R^{n-k-2}) & H^p(B, P^{n-k-2}) & \xrightarrow{d_3} & H^{p+3}(B, R^{n-k-4}) \\ \downarrow L^{k+1} \cong 0 & & \cong \downarrow L^{k+1} & \& & L \downarrow \text{onto} \quad \text{curved arrow} \quad \downarrow L \\ H^p(B, R^{n+k}) & \xrightarrow{d_3} & H^{p+3}(B, R^{n+k}) & H^p(B, L P^{n-k-2}) & \xrightarrow{d_3} & H^{p+3}(B, R^{n-k-2}) \end{array}$$

$\Rightarrow$  As before,  $d_3 = 0$ . Continue &  $d_m = 0$  for all  $m$ .  $\sqcup$