



⇒ By Riemann extension theorem (Pg), we can extend the holomorphic function to $\{(z_1, z_2) : |z_1| \leq \delta, |z_2| \leq \epsilon\}$.

⇒ Since the graph of a holomorphic function is an analytic variety, on $\{(z_1, z_2) : |z_1| < \delta, |z_2| < \epsilon\}$, a set of a finite number of points \cup the graph is analytic variety.

$$\{(z_1, f(z_1)) : |z_1| < \delta\} = (z_2 - f(z_1) = 0) \quad \square$$

In general we use the by-now-familiar argument involving the elementary symmetric functions: set

$$\begin{aligned} \varphi_i(z) &= \frac{1}{2\pi\sqrt{-1}} \int_{|z_2|=\epsilon} z_2^i \frac{dh(z_1, z_2)}{h(z_1, z_2)} \\ &= \sum_{j=1}^d z_{2,j}(z_1)^i, \end{aligned}$$

where $\pi^{-1}(z_1) = \{(z_1, z_{2,j}(z_1))\}_{j=1}^d$.

$$\begin{aligned} \varphi_i(z) &= \frac{1}{2\pi\sqrt{-1}} \int_{|z_2|=\epsilon} z_2^i \frac{dh(z_1, z_2)}{h(z_1, z_2)} \\ &= \frac{1}{2\pi\sqrt{-1}} \sum_{j=1}^d \int_{\partial B_\delta(z_{2,j}(z_1))} z_2^i \frac{dz_2}{z_2 - z_{2,j}(z_1)} = \frac{1}{2\pi\sqrt{-1}} \sum_{j=1}^d z_{2,j}(z_1)^i \quad \square \end{aligned}$$