

Remark: $M \subset N$ subspace \mathcal{F} sheaf on M .

We can extend \mathcal{F} by zero to obtain a sheaf $\tilde{\mathcal{F}}$ on N , setting

$$\tilde{\mathcal{F}}(U) = \mathcal{F}(U \cap M).$$

and letting the restriction maps be the obvious ones. Thus we consider \mathcal{F} as a sheaf on either M or N .

Examples

1. On any complex manifold,

$$0 \rightarrow \mathbb{Z} \xrightarrow{\bar{i} \rightarrow \text{inclusion}} \mathcal{O} \xrightarrow{\exp} \mathcal{O}^* \rightarrow 0 \text{ is exact.}$$

This fundamental sequence is called the exponential sheaf sequence.

$$\ker \exp = \text{im } \bar{i}.$$

$$\textcircled{1} \text{im } \bar{i} \subset \ker \exp$$

$$\exp(\bar{i}(U)(n)) = e^{2\pi i n} = 1 \Rightarrow \bar{i}(U)(n) \in (\ker \exp)(U).$$

$$\textcircled{2} \ker \exp \subset \text{im } \bar{i}.$$

$$(U, \sigma), \sigma \in \mathcal{O}(U).$$

$$p \in U.$$

$$\exp(\sigma) = 0 = \exp^{2\pi i \sigma} = 1 \Rightarrow \sigma \text{ is integer valued}$$

$$\Rightarrow \exists \text{ a contractible open set } V_p \subset U \text{ s.t.}$$

$$f \in \mathcal{O}(V_p) \text{ s.t. } f = \sigma \text{ on } V_p.$$

func and
 σ is continuous
 $\Rightarrow \sigma = \text{const.}$

$$\text{im } \exp = \mathcal{O}^*.$$

Given $f \in \mathcal{O}^*(U)$, $\exists V_p$ s.t. $\exists g$ s.t. $\exp g = f$

If V_p is contractible, it is possible.