

$$\begin{aligned}\sigma_2(V_2) &= \{ \Lambda : \dim(\Lambda \cap \overline{V}_{k+i-c_i}) \geq i \} \\ &= \{ \Lambda : \dim(\Lambda \cap \overline{V}_3) \geq 1 \} = \{ \Lambda : \Lambda \cap V_2 \neq \emptyset \}.\end{aligned}$$

$$\dim \sigma_2 = \dim \sigma_{1,1} = p-2 = 6.$$

$$\#(\sigma_{2,1} \cdot \sigma_{2,1} \cdot \sigma_{1,1})_{G(2,6)} \quad k=2, n=6.$$

$$\text{Choose } \alpha=2, \beta=0, \gamma=0 \Rightarrow a_2=1 \quad b_0=4=c_0$$

$$\text{and } \alpha+\beta+\gamma=k=2. \Rightarrow \text{By the Reduction formula I,}$$

$$\#(\sigma_{2,1} \cdot \sigma_{2,1} \cdot \sigma_{1,1})_{G(2,6)}$$

$$= \#(\sigma_1 \cdot \sigma_{2,1} \cdot \sigma_{1,1})_{G(2,5)}$$

$$\text{Choose } \alpha=0, \beta=2, \gamma=0 \Rightarrow a_0=3 \quad b_2=1 \quad c_0=3$$

$$\text{and } \alpha+\beta+\gamma=2. \Rightarrow \text{Again by the Reduction formula II,}$$

$$\#(\sigma_1 \cdot \sigma_{2,1} \cdot \sigma_{1,1})_{G(2,5)}$$

$$= \#(\sigma_1 \cdot \sigma_1 \cdot \sigma_{1,1})_{G(2,4)}$$

$$= \#(\sigma_1 \cdot \sigma_1 \cdot \sigma_0)_{G(2,3)} \text{ by the Reduction formula II}$$

$$(\alpha=\beta=0 \quad \gamma=2)$$

$$= \#(\sigma_1 \cdot \sigma_1)_{G(2,3)} \text{ since } \sigma_0 = G(2,3)$$

$$= 1 \text{ since } a_i + b_{2-i+1} = 1 \Leftrightarrow a_i + b_{3-i} = 1$$

$$\text{by the formula on P198.}$$

$$\#(\sigma_{2,1} \cdot \sigma_{2,1} \cdot \sigma_2)_{G(2,6)} \quad (\text{R.F II})$$

$$= \#(\sigma_{2,1} \cdot \sigma_1 \cdot \sigma_2)_{G(2,5)} \quad \alpha=\gamma=0, \beta=2$$

$$= \#(\sigma_1 \cdot \sigma_1 \cdot \sigma_2)_{G(2,4)} \text{ by R.F II } \alpha=2, \beta=\gamma=0$$

$$= \#(\sigma_1 \cdot \sigma_0 \cdot \sigma_1)_{G(2,3)} \left(\text{by choosing } \alpha=0, \beta=\gamma=1 \right.$$

$$a_0=2 \quad b_1=1 \quad c_1=2 \Rightarrow 5 \geq 2+2+1.$$

$$= \#(\sigma_1 \cdot \sigma_1)_{G(2,3)} = 1$$

Thus we can write