

similar to the one encountered in the lemma in the discussion concerning the intrinsic form of local duality in Section 3 above. Recall that $\text{Ext}^*(M; \mathcal{O}_X, \Omega^n)$ is the hypercohomology of the complex of sheaves

$$\underline{\text{Hom}}_{\mathcal{O}}(\mathcal{O}, \Omega^n) \rightarrow \underline{\text{Hom}}_{\mathcal{O}}(\Omega^1, \Omega^n) \rightarrow \dots$$

For the commutative diagram, see P688 & P690. \Rightarrow

Using the identifications provided by the commutative diagram, we write this complex of sheaves as Ω^{n-} . Thus

$$\text{Ext}^*(M; \mathcal{O}_X, \Omega^n) \cong H^*(M, \Omega^{n-}).$$

$$\begin{array}{c} \text{For} \\ \text{Hom}(E, \Omega^n) \end{array} \quad \underline{\text{Hom}}_{\mathcal{O}}(\mathcal{O}, \Omega^n) \rightarrow \underline{\text{Hom}}_{\mathcal{O}}(\Omega^1, \Omega^n) \rightarrow \dots$$

$$\begin{array}{ccc} \downarrow & & \downarrow \\ \Omega^{n-} : \Omega^n & \rightarrow & \Omega^{n-1} \rightarrow \dots \end{array}$$

$$\Rightarrow \text{Ext}^*(M; \mathcal{O}_X, \Omega^n) = H^*(M, \text{Hom}(E, \mathcal{O}), \Omega^n) \cong H^*(M, \Omega^{n-}) \quad \Rightarrow$$

We note that the differential used to calculate the hypercohomology on the right is $\delta \pm U(V)$, where δ is the Čech coboundary mapping.

Now, according to the general discussion of hypercohomology there are two spectral sequences $\{{}^i E_r\}$ and $\{{}^i E_r'\}$ abutting to $H^*(M, \Omega^{n-})$. One of them has