

$$\Rightarrow \underline{\text{Ext}}_0^0(f_Z, \wedge^n \mathcal{E}^*) = \underline{\text{Hom}}(f_Z, \wedge^n \mathcal{E}^*) \cong \wedge^n \mathcal{E}^*.$$

$$E_2^{n,0} = H^n(M, \wedge^n \mathcal{E}^*).$$

$$\begin{array}{c} E_2^{n-2,-1} \\ \parallel \\ 0 \end{array} \longrightarrow E_2^{n,0} \longrightarrow E_2^{n+2,1} \parallel_0 \Rightarrow E_3^{n,0} = E_2^{n,0} = E_4^{n,0} = \dots = E_n^{n,0}$$

$$\begin{array}{c} E_{n-1}^{1,n-2} \\ \parallel \\ E_2^{1,n-1-1} \end{array} \longrightarrow E_{n-1}^{n,0} \longrightarrow E_{n-1}^{2n-1,1} \parallel_0 \Rightarrow H^1(M, \underline{\text{Ext}}_0^{n-2}(f_Z, \wedge^n \mathcal{E}^*)) = 0$$

□

For each $p \in Z$ there is an induced local extension class

$$e_p \in \underline{\text{Ext}}_0^{n-1}(f_Z, \wedge^n \mathcal{E}^*)_p,$$

where $\bigoplus_{p \in Z} e_p \in H^0(M, \underline{\text{Ext}}_0^{n-1}(f_Z, \wedge^n \mathcal{E}^*))$ is the image of e , and therefore satisfies

$$d_n \left(\bigoplus_{p \in Z} e_p \right) = 0 \quad \text{in } H^1(M, \wedge^n \mathcal{E}^*).$$

We will interpret this relation as a residue theorem.

□ By the explanation on p127,

$$\begin{array}{ccc} \text{Ext}^{n-1}(M; f_Z, \wedge^n \mathcal{E}^*) & \longrightarrow & \underline{\text{Ext}}_0^{n-1}(f_Z, \wedge^n \mathcal{E}^*)_p \\ \downarrow e & \xrightarrow{\quad} & \downarrow e_p \\ H^0(M, \underline{\text{Ext}}_0^{n-1}(f_Z, \wedge^n \mathcal{E}^*)) & = & \bigoplus_{p \in Z} \underline{\text{Ext}}_0^{n-1}(f_Z, \wedge^n \mathcal{E}^*)_p \end{array}$$