

There are two spectral sequences, $\{E_r\}$ and $\{E_r'\}$, both abutting to $H^*(K^*)$. By symmetry we may consider the first one. Then

$$E_0^{p,q} = \frac{K^{p,q} + K^{p+1,q-1} + \dots}{K^{p+1,q-1} + \dots} \cong K^{p,q}.$$

$$\begin{aligned} \mathbb{F} \quad E_0^{p,q} &= \frac{F^p K^{p,q}}{F^{p+1} K^{p,q}} = \frac{\bigoplus_{\substack{p' \geq p, p'+q' = p+q \\ p'+q' = p+q \\ p' \geq p+1}} K^{p',q'}}{\bigoplus_{\substack{p'+q' = p+q \\ p' \geq p+1}} K^{p',q'}} \\ &= \frac{K^{p,q} \oplus K^{p+1,q-1} \oplus \dots}{K^{p+1,q-1} \oplus \dots} = K^{p,q} \quad \Rightarrow \end{aligned}$$

The differential d_0 is induced from $D = d + \delta$ by passing to the quotient. Thus, under the above isomorphism $d_0 = \delta$ and

$$E_1^{p,q} \cong H_{\delta}^q(K^{p,*}),$$

where the right-hand side denotes the q th cohomology group of the complex

$$\dots \rightarrow K^{p,q-1} \xrightarrow{\delta} K^{p,q} \xrightarrow{\delta} K^{p,q+1} \rightarrow \dots$$

$$\mathbb{F} \quad \begin{array}{ccc} E_0^{p,q} & \xrightarrow{D=d+\delta} & E_0^{p,q+1} \\ \parallel & & \parallel \\ K^{p,q} & \xrightarrow{\delta} & K^{p,q+1} \end{array} = \frac{F^p K^{p,q+1}}{F^{p+1} K^{p,q+1}}$$

For example, $p=q=2$,

$$\frac{K^{2,2} \oplus K^{3,1} \oplus K^{4,0}}{K^{3,1} \oplus K^{4,0}} \xrightarrow{D=d+\delta} \frac{K^{2,3} \oplus K^{3,2} \oplus K^{4,1} \oplus K^{5,0}}{K^{3,2} \oplus K^{4,1} \oplus K^{5,0}} = K^{2,3}$$