

Recall that the α -planes $\{\sigma(p)\}_{p \in x}$ lying in $T_x(G) \cap G$ are spanned by x together with the lines of one of the rulings of Q , while the planes $\{\sigma(h)\}_{h \in x}$ are spanned by x and the lines of the other ruling of Q .

Γ Q is a smooth quadric in $\mathbb{P}^3 \Rightarrow Q$ has two families of lines. \Rightarrow See P758~P759 for the rest.

\sqcup

Now if $T_x(F)$ is tangent to G at some point y , we may take $y \in H$, so that the locus $T_x(F) \cap T_x(G) \cap G$ consists of the two α -planes $\sigma(p)$ and $\sigma(h)$ spanned by x and the two lines of intersection $Q \cap T_x(F)$. (See Figure 15.)

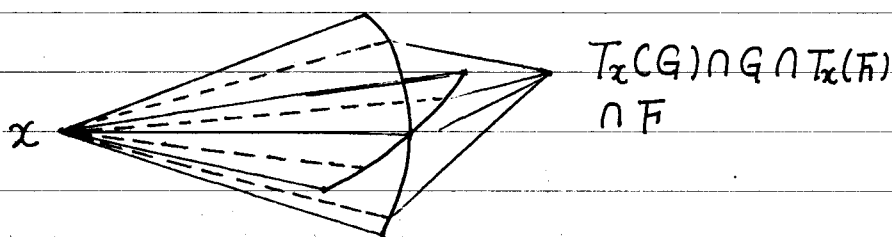


Figure 15. $T_x(G) \cap G \cap T_x(F)$ if $x \in Z$.

Γ Since $x \neq y$, we may choose a hyperplane $H \ni y$. $\Rightarrow Q = T_x(G) \cap G \cap H$ is a smooth quadric in $\mathbb{P}^3 \Rightarrow Q \cap T_x(F) = Q \cap T_y(G)$ is a singular quadric in \mathbb{P}^2 , which is the union of two lines (distinct). Clearly, $\sigma(p), \sigma(h) \subset T_x(F) \cap$