

holds for every vector  $\vec{\lambda}$ .

⌈ (5) and (6) are the difference between Def. 1 & Def. 1',

We pick the values

$$\begin{aligned} a_p^1 &= \lambda_p = \alpha_p^1, \quad 1 \leq p \leq n \\ a_p^{\bar{j}} &= \sigma \alpha_p^{\bar{j}}, \quad \bar{j} \geq 2, \quad 1 \leq p \leq n. \end{aligned} \quad (7)$$

$\sigma$  being a variable number which will be made to tend to 0 and the  $\alpha_p^{\bar{j}}$  being chosen in such a way that the square matrix  $\|\alpha_p^{\bar{j}}\|$  is regular; the same is true for the matrices  $\|a_k^{\bar{j}}\|$  when  $\sigma \neq 0$ .

$$\left( \begin{array}{ccc} \alpha_1^1 & \dots & \alpha_1^n \\ \vdots & & \vdots \\ \alpha_n^1 & \dots & \alpha_n^n \end{array} \right) = \left( \begin{array}{ccc} a_1^1 & \dots & a_1^n \\ \frac{a_2^1}{\sigma} & \dots & \frac{a_2^n}{\sigma} \\ \vdots & & \vdots \\ \frac{a_n^1}{\sigma} & \dots & \frac{a_n^n}{\sigma} \end{array} \right) \Rightarrow \det(\alpha_i^{\bar{j}}) = \frac{1}{\sigma^{n-1}} \det$$

$(a_i^{\bar{j}}) \Rightarrow$  Regular means that  $\det \neq 0$ .  $\Downarrow$

Writing (6) with the values given by (7), we get

$$T(V, \vec{\lambda}) + |\sigma|^2 \sum_{\bar{j}=2}^n T(V, \vec{a}^{\bar{j}}) \geq 0.$$

$$\left\{ \Delta_{\vec{z}'} V = \sum_{\bar{j}} T(V, \vec{a}^{\bar{j}}) = T(V, \vec{a}^1) + T(V, \vec{a}^2) + \dots + T(V, \vec{a}^n) \right.$$

$$\Rightarrow T(V, \vec{a}^1) = T(V, \vec{\lambda}), \quad T(V, \vec{a}^{\bar{j}}) = \sum \frac{\partial^2 V}{\partial z_p \partial \bar{z}_q} \sigma \alpha_p^{\bar{j}} \bar{\sigma} \bar{\alpha}_q^{\bar{j}}$$