

$$\begin{pmatrix} a_1 & b_1 & c_1 & * & \dots \\ a_2 & b_2 & c_2 & & \\ a_3 & b_3 & c_3 & & \\ \vdots & \vdots & \vdots & & \end{pmatrix} \text{ has rank } n-l \text{ and } (p-l) \times (q-l) \text{ matrix.}$$

To make  $M$  rank  $n+k$ , we have only to make  $N$  rank  $n+k-l$ , which is easy.

Note that when we change vectors slightly,  $e^i$ 's are not involved ( $\therefore \begin{pmatrix} 0 \\ \vdots \\ 1 \\ \vdots \\ 0 \end{pmatrix}$  type.)

$$\begin{aligned} v_1 &= (* \dots * \overset{n-k+1-a_1}{\downarrow} 1, 0 \dots 0 \ 0 \\ v_2 &= (* \dots * \ 0 \ * \dots \overset{n-k+2-a_2}{\uparrow} 1, 0 \dots 0 \\ v_3 &= (* \dots * \ 0 \ * \dots \ 0 \ * \dots \overset{n-k+3-a_3}{\uparrow} 1, 0 \dots \end{aligned}$$

Conversely, any matrix of this form describes a  $k$ -plane  $\Lambda \in W_{a_1 \dots a_k}$ .  $\square$  O.K.  $\cup$

Since  $(k^2 + \sum a_i)$  entries are specified in the diagram and the rest are completely free to vary, we have homeomorphisms

$$W_{a_1, a_2, \dots, a_k} \cong \mathbb{C}^{k(n-k) - \sum a_i};$$

Consequently, the sets  $W_{a_1 \dots a_k}$  give a cell decomposition of  $G(k, n)$ .

$\square$  For  $v_1$ ,  $n - (n-k+1-a_1) + 1$  entries  
for  $v_2$ ,  $n - (n-k+2-a_2) + 1 + 1$  entries  
for  $v_3$ ,  $n - (n-k+3-a_3) + 1 + 2$  "