

the original one by a transformation (T) defined by

$$\omega_k' = \sum_j C_k^j \omega_j; \quad \bar{\omega}_k' = \sum_j \bar{C}_k^j \bar{\omega}_j, \quad C_k^j \in K \quad (3)$$

and commuting with the involution, will be called "admissible": such transformations (T) form a group G . By the definition the positive elements of E_{2n} of degree zero are the positive real constants $a \in \mathbb{R}^+$. Further, we will consider a fundamental form

$$\tau_n = C (\bar{\omega}_1 \wedge \omega_1) \wedge \dots \wedge (\bar{\omega}_n \wedge \omega_n), \quad (4)$$

where $C \in \mathbb{R}^+$.

In the passage to another admissible basis $(\omega', \bar{\omega}')$, C is replaced by C' in (4) where again $C' \in \mathbb{R}^+$. Every element $\alpha \in E_{2n}$ which can be written as $\alpha = \sum a_k \omega_k$, $a_k \in K$, will be called purely linear.

Definition An element $\phi \in E_{2n}$ is called positive of degree p , $0 \leq p \leq n$, if

a) ϕ is homogeneous of type (p, p) .

b) for each system $L^{n-p} = (\alpha_1, \alpha_2, \dots, \alpha_{n-p})$ of purely linear elements one has

$$\phi \wedge (\bar{\alpha}_1 \wedge \alpha_1) \wedge \dots \wedge (\bar{\alpha}_{n-p} \wedge \alpha_{n-p}) = l(\phi, L^{n-p}) \tau_n$$

with $l(\phi, L^{n-p}) \in \mathbb{R}^+$.

Consequences.

(1) The set E_+^p of positive elements of degree p is