

92, 12, 25

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⇒ We can consider a holomorphic map $f: V \rightarrow \mathbb{P}^2$.

Let $U_0 = (W_0 \neq 0)$, $U_1 = (W_1 \neq 0)$ and $U_2 = (W_2 \neq 0)$.

$$\begin{array}{ccccc} f^{-1}(U_0) & \xrightarrow{f} & U_0 \subset \mathbb{P}^2 & \longrightarrow & \mathbb{C}^2 \\ \downarrow & & \downarrow & & \downarrow \\ \mathbb{C} & \longrightarrow & [1, f_{01}(z), f_{02}(z)] & \longrightarrow & (f_{01}(z), f_{02}(z)) \end{array}$$

$$\begin{array}{ccccc} f^{-1}(U_1) & \xrightarrow{f} & U_1 \subset \mathbb{P}^2 & \longrightarrow & \mathbb{C}^2 \\ \downarrow & & \downarrow & & \downarrow \\ \mathbb{C} & \longrightarrow & [f_{11}, 1, f_{12}] & \longrightarrow & (f_{11}(z), f_{12}(z)) \end{array}$$

$$\begin{array}{ccccc} f^{-1}(U_2) & \longrightarrow & U_2 \subset \mathbb{P}^2 & \longrightarrow & \mathbb{C}^2 \\ & & & & \downarrow \\ \mathbb{C} & \longrightarrow & [f_{21}, f_{22}, 1] & \longrightarrow & (f_{21}(z), f_{22}(z)) \end{array}$$

$$\Rightarrow \frac{f_{11}}{1} = \frac{1}{f_{01}} = \frac{f_{12}}{f_{02}}, \quad \frac{f_{21}}{f_{11}} = \frac{f_{22}}{1} = \frac{f_{02}}{f_{01}}, \quad \frac{1}{f_{21}} = \frac{f_{01}}{f_{22}} = \frac{f_{02}}{1} \quad (*)$$

Question: f_{01} can be extended to V as a meromorphic function?

on U_1 , from $(*)$, $f_{01} = \frac{1}{f_{11}}$

on U_2 , " $f_{01} = \frac{f_{22}}{f_{21}}$

On $U_1 \cap U_2$, since $\frac{f_{21}}{f_{11}} = \frac{f_{22}}{1}$, $\frac{1}{f_{11}} = \frac{f_{22}}{f_{21}}$.