

cible at 0. $n = k$. $V_i' = V_j$ for some j . i.e.
 $V = V_1 \cup \dots \cup V_k$ is unique.

pf). By the proper mapping theorem, $\pi(V_i)$ is a subvariety of \mathbb{C}^{n-1} . $\Rightarrow \pi(V_i)$ is irreducible, otherwise V_i is irreducible. $\Rightarrow \pi(V_i) = W_i$ for some i . Similarly, we have $\pi(V_j) = W_m$ for some m .

Suppose $V = V_1' \cup \dots \cup V_n'$.
 $\Rightarrow \pi(V_1')$ is irreducible \Rightarrow If $\pi(V_1') = W_1$,
 $\pi^{-1}(W_1) = V_1' \cup \dots = V_1 \cup \dots$.

$\frac{1}{z} > 0$ $\frac{1}{z}$ or $\frac{1}{z}$ is the assertion $1 \neq 0$ \Rightarrow See p98. Whitney.

Finally, several more fundamental results in several complex variables will be proved by the methods of residues in Chapter 5.

p20

Definition: An analytic subvariety V of a complex manifold M is a subset given locally as the zeros of a finite collection of holomorphic functions. A point $p \in V$ is called a smooth point of V if V is a submanifold of M near p , that is, if V is given in some nbd of p by holomorphic functions f_1, \dots, f_k with $\text{rank } J(f) = k$; the locus of smooth points