

$$\Rightarrow \chi(\mathcal{O}_M) = \sum_{v(p)=0} \frac{1}{\det A_p} (-1)^n \frac{\det A_p}{\det(I - e^{-tA_p})} \xrightarrow{\text{my L.F.F.}}$$

$$= \sum_{v(p)=0} \frac{1}{\det A_p} (-1)^n (-1)^n t^{-n} \sum_i (-1)^i \text{Td}_i(p^1, \dots, p^n) t^i$$

$$= (-1)^n t^{-n} \sum_i \left\{ \sum_{v(p)=0} (-1)^i \text{Td}_i(p^1, \dots, p^n) / \det A_p \right\} t^i$$

$$\Rightarrow \chi(\mathcal{O}_M) = (-1)^n \text{Td}_n(p^1, \dots, p^n) \\ = (-1)^n \text{Td}_n(c_1, \dots, c_n)$$

Again different from the book.

$$\chi(\mathcal{O}_M) = \sum_{v(p)=0} \frac{1}{\det A_p} \frac{\det A_p}{\det(I - e^{tA_p})}$$

$$= \sum_{v(p)=0} \frac{1}{\det A_p} t^{-n} \sum_i \text{Td}_i(p^1, \dots, p^n) t^i$$

$$= t^{-n} \sum_i \left\{ \sum_{v(p)=0} \text{Td}_i(p^1, \dots, p^n) / \det A_p \right\} t^i$$

$$\Rightarrow \chi(\mathcal{O}_M) = \text{Td}_n(c_1, \dots, c_n). \checkmark \text{ the same as the book.}$$

We had better define the Todd polynomials by

$$\frac{\det A}{\det(I - e^{-tA})} = t^{-n} \left\{ \sum_i \text{Td}_i(p^1(A), \dots, p^i(A)) t^i \right\}$$

as on p152 Wells.

⇒

For a curve, the formula reads

$$\chi(\mathcal{O}_M) = \frac{1}{2} c_1(M),$$